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## MASTER RESEARCH PROJECT

Radio continuum in HI-selected galaxies from the Apertif surveys

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## Abstract

I present a comparative analysis of star formation rate (SFR) tracers, at different electromagnetic bands, in a sample of HI-selected galaxies taken from Apertif HI survey. In addition to the presence of atomic gas, I require them to also have a radio continuum (RC) counterpart, performing a cross match with the Apertif DR1 catalog. I get their corresponding infrared (IR) data from WISE survey and I later use information with improved extended source photometry (T. Jarrett, priv. comm.). The purpose of this study is to explore the consistency of SF tracers at different bands, test the far-IR-Radio correlation and see how well radio continuum works as a SF tracer in dwarf galaxy regimes. I performed a visual inspection procedure, aimed at identifying possible AGN contaminations that often occur in the radio band. As a result, I created a subsample of galaxies having a good match of RC contours with the shape of the source as seen in WISE W1 photometry. Then, I investigated the relations of SFRs at different IR bands with the RC based one. Finally, I performed a further comparison with the far-ultraviolet (FUV) SFR tracer derived from GALEX data. The trends between the WISE W3 (12 $\mu$ m) and W4 (22 $\mu$ m) band derived SFRs and the RC SFRs are relatively tight linear relations. However, when using the mid-IR SF tracer, derived from a combination of W3 and W4, including a correction calibrated from galaxies with FUV data to account for the typical low dust content of smaller galaxies, the IR SFR vs RC SFR trend clearly deviates from a one-to-one line, with a discrepancy at small values. The final FUV test has not confirmed the reliability of the RC or IR tracers at lower SFR values. Therefore, further investigations are advisable, for example using improved Apertif data products and a more dwarf-dominated sample.

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## **Acknowledgements**

I would like to thank my supervisor, Dr. Betsey Adams, for guiding me through the project and for her invaluable advice on the research subject as well as on the general approach to the analysis. From this collaboration, I learn not only science but also scientific method.

I am deeply grateful to Prof. Thomas Jarrett who kindly provided me with data and information that were essential to my study.

I also want to express my sincere appreciation to scientists from ASTRON who have contributed to my work sharing new data and suggestions.

I would like to thank Kim W. who has always supported me along the way.

## CHAPTER 1: INTRODUCTION

### 1.1 GALAXIES

Galaxies are cosmic objects, each containing dark matter, gas, dust and millions or billions of stars, bound together by gravity. Nowadays, we know that the Universe is filled with more than two trillion galaxies out to very large distances (Conselice et al. 2016). The astronomer Edwin Hubble, back in 1926, set up a system to classify galaxies according to their morphologies (Hubble E.P. 1926); this classification is still used at present days with some modifications and additions. The three main categories in the Hubble system (Figure 1) are:

- **Elliptical galaxies**, relatively featureless and spherical. These are indicated with the letter "E" and they are divided into subclasses based on how round they appear.
- **Spiral Galaxies**, with very distinctive arms out from their centers. These are distributed into two subclasses, regular spirals (S) and barred spirals (SB), the latter includes our Milky Way. Both regular and barred spirals have a spherical bulge of stars at their centers surrounded by a thin rotating disk of stars that contains many spiral arms. The two main subclasses of spirals are further divided into sub-categories depending on how prominent the spiral arms appear.

Lenticular galaxies appear to be an intermediate class between most flattened ellipticals and the most tightly compact spirals. They show clear signs of a disk and a central bulge but they have no spiral arms and little interstellar gas.

- **Irregular galaxies** are all the ones that do not fit the other two main classes. These present mixed features of ellipticals and spirals with no clear structures and shapes. These are mostly star forming galaxies.

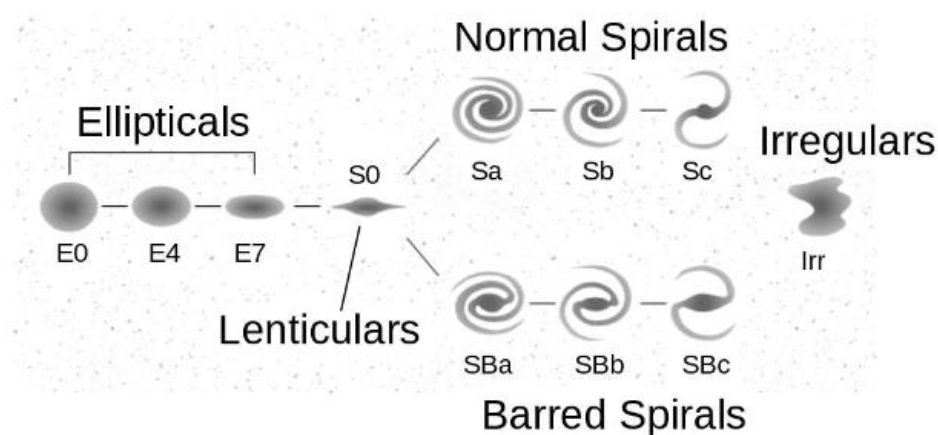


Figure 1: The Hubble classification schema for galaxies

There is a correlation between the physical differences of galaxies and the different Hubble types (Kennicutt 1998). One such property is the angular momentum, related to the rate at which the various parts of the galaxy rotate about the centre, and its degree of compactness. Overall, the angular momentum per unit mass of elliptical and irregular galaxies is low, whereas it is relatively high for spirals and lenticulars (Ogle P.M. et al. 2019).

Another property correlated with Hubble class concerns the ratio of the mass gas to the total mass of stars in a galaxy. And specifically, the presence of molecular or atomic gas determines other important characteristics such as the mass, luminosity and size of galaxies. This is because there is a linear proportionality between the surface density of the star formation rate (SFR) with the surface density of molecular hydrogen (Schruba et al. 2010).

Ellipticals contain many old stars and a very little gas between them; thus, they lack the raw ingredients to make new luminous stars and consequently they do not look as bright as other galaxy types per unit stellar mass. Ellipticals are therefore called *dying galaxies* and they are the most commonly observed. Their masses vary from  $10^9$  to over  $10^{13} M_{\odot}$  (Longair 2007).

Spiral galaxies have a mix of young and old stars as there is a significant amount of gas and dust that fill the disk; thus in the disk new star formation takes place continuously (Salim S. et al. 2007). Spirals have a narrow range of masses, from  $10^9$  to a few times  $10^{12} M_{\odot}$ .

Whereas irregular galaxies are simply more chaotic, they can be very bright and host many young stars. They exhibit an intermediate range of properties, with masses from  $10^7$  to  $10^{10} M_{\odot}$ .

Galaxies do not appear the same way they formed. They can change over cosmic time as a result of interactions, collisions and mergers between them (Hernquist 1995). Such interactions of galaxies trigger bursts of star formation and change their own characteristics in a process known as galaxy evolution.

#### 1.1.1. GALAXY FORMATION IN A NUTSHELL

To the best of our knowledge, galaxy formation begins when dark matter merges and assembles in small objects, called dark matter halos, that later, grow up to build larger halos in a hierarchical way. As these structures expand with time, the present gas and dust components start to create luminous stars. The latter evolve and die cyclically to form new star generations (Cattaneo A. et al. 2011), bound into larger systems: galaxies.

Also galaxies are thought to grow up hierarchically: scientists have proved that most of earlier galaxies tend to be smaller and more irregular than the present-day ones (Cole S. et al. 2000). However, this is not univocal, as some distant galaxies appear similar to the ones nearby.

## 1.2 DWARF GALAXIES

Dwarf galaxies constitute the largest subset of galaxies in the Universe (Cross et al. 2004); they have a great cosmological importance as considered to have been the first to form and then merged, in hierarchical scenarios, to create bigger galaxies. Dwarfs are metal-poor systems thus, very appealing to astronomers as assumed to be highly unevolved and excellent laboratories to study primordial conditions (Tolstoy et al. 2009). However, they are not well understood as small and faint. They may also contain a larger amount of dark matter than of luminous masses (Lee J et al. 2009). These “tiny” systems have low masses ( $M \leq 10^9 M_{\odot}$ ), low metallicity ( $[Fe/H] < -3$ ) (Simon J.D. 2019) and relatively low luminosity ( $\sim 10^9 L_{\odot}$ ).

Like normal galaxies, also dwarfs can be classified into subclasses; the two main ones are:

- Late-type galaxies, star forming systems → dwarf irregular galaxies (dIs) and blue compact dwarf (BCD) galaxies;
- Early-type systems, not currently forming stars → dwarf ellipticals (dEs) and dwarf spheroidals (dSphs) with the recent addition of ultra-faint dwarf galaxies that are mostly like dSphs, but noted for their extremely faint luminosities.

dIs are particularly interesting because they are characterized by recent star formation. They have irregular visual appearance, large HI (atomic hydrogen) gas reservoirs (Hoffman G. et al. 1996) and low dust content (Calzetti 2001). Their morphology is chaotic with a lack of spiral structures and active star formation across the whole galaxy (Hunter 1997). dIs and BCDs are very similar but the latter have a higher star formation rate (Papaderos et al. 1994). Whereas, dwarf ellipticals (dEs) and dwarf spheroidals (dSphs) mostly contain old stars, and low gas content, therefore not ongoing or recent star formation (Ferguson & Binggeli 1994). These two subclasses slightly differ in mass (Han et al. 1998).

## 1.3 STAR FORMATION

Stars form in dense interstellar clouds, composed of molecular hydrogen ( $H_2$ ). The process begins when the gas cools down under 100 Kelvin and consequently undergoes a gravitational collapse turning into stellar mass.  $H_2$  is particularly efficient in forming stars as it can cool down significantly: its roto-vibrational transitions cause energy loss thus, gas cooling (Longair 2007). The dust component of galaxies, mostly provided by supernovae explosions, is a crucial player in the star formation (SF) processes as it helps  $H_2$  to form on dust grains (Calzetti 2007). Furthermore, dust is responsible for the absorption and reprocessing of the ultraviolet (UV) and visible light, emitted by the newborn massive stars, into the infrared (IR) range. This last concept will be further analyzed in the next subsection.

Measuring the rate at which a galaxy forms its stellar mass - the star formation rate SFR - is essential to know the physical processes in galaxy evolution; therefore, it is a distinctive property of different galaxy types. SFRs are measured in units of  $M_{\odot}/yr$ . When stars form, depending on their intrinsic characteristics (mass, temperature and size), they can emit radiation at different wavelengths; therefore, SF processes can be traced using different indicators (Kennicutt et al. 2009; Calzetti 2012). The basic idea behind the SFR measurement is to analyse the galaxy fluxes, at specific wavelengths, in a way to disentangle the stellar



continuum or the emission line of recently formed stars from the contributions of older stellar populations (Calzetti et al. 2007). More massive stars, O and B, burn their fuel at a higher speed, hence they have a shorter lifetime ( $\leq 3 \times 10^7$  yrs). For this reason they are the most studied to measure the galaxy SFR as they simply formed “more recently” with respect to the others, tracing a recent SF activity.

A key ingredient in SF activity is the initial mass function IMF as it specifies the number of stars in a certain mass range for a freshly formed stellar population (Carigi 2011). Therefore, the IMF gives clues on how many massive young stars form in a specific event. The IMF is a mathematical expression; the most popular is the form of a power law (Salpeter 1955) or a combination of power laws (Kroupa et al. 1993) that describes the mass-spectrum of stars born collectively in “one event”.

#### 1.4 STAR FORMATION TRACERS

Galaxies can be very diverse in forms and shapes as well as stellar populations, star forming activity and interstellar medium (ISM) properties. Therefore, their SFR can be traced using different indicators.

The H $\alpha$  emission line and the ultraviolet (UV) flux are important SFR tracers. In particular, the first one originates from the recombination of the ionized hydrogen gas of nebular clouds by the starlight of the most massive O and B type stars ( $M \gtrsim 17 M_{\odot}$ ); it therefore traces star formation activity occurring over a few million years that corresponds to the lifetime of these star classes. Whereas, the UV light comes directly from the photosphere of stars in a larger mass range ( $M \gtrsim 3 M_{\odot}$ ) hence it traces star formation activity over longer timescales  $\sim 10^8$  yr (Lee J.C. et al. 2009). However, the UV light is extinguished by dust and re-emitted at infrared (IR) wavelengths (Reddy et al. 2015) while the H $\alpha$  emission line is less attenuated (Kewley et al. 2002).

Due to the dust extinction effects just mentioned, the IR band offers reliable tracers of SF, in relation to the dust content in galaxies and the dust opacity. It is important to mention that both massive short-lived stars and low-mass, long-lived stars can heat the dust. In particular, the galaxy luminosity at mid/far-IR (MIR, FIR) wavelengths ( $\sim 5\text{-}1000 \mu\text{m}$ ), indicated as  $L_{TIR}$ , probes the dust heated by young (1-100 Myrs) UV luminous O and B stars as well as intermediate mass stars.

In addition, SFR can be also traced from radio continuum (RC) emission (Condon 1992). There are two different components of radio luminosity in a galaxy. One is given by the thermal bremsstrahlung from ionized hydrogen in HII regions, which directly tracks forming stars as the amount of ionized hydrogen reflects the ionizing luminosity of the very young stellar populations. The second component is the non-thermal synchrotron emission from cosmic ray electrons (CRE) spiraling in the galactic magnetic field (Condon 1992). In principle, at the end stage of their lifetime, massive stars produce Type II supernovae whose remnants (SNRs) are responsible for accelerating relativistic electrons in galaxies. Since these very massive stars have a short duration, also their relativistic electrons live for a relatively small period of time ( $< 10^8$  yrs) thus, they can trace a recent SF activity (Vollmer B. et al. 2022). A good advantage of using RC emission as a SFR indicator is that radio observations are not affected by the light of older stellar populations nor by dust. However, a big limitation of RC SFR tracers is the interference from the bright

radio luminosity of active galactic nuclei (AGNs) or Type Ia supernovae that come from long lived stars (Radcliffe J.F. et al. 2021).

In order to test the reliability of individual SFR tracers, a widely used approach is to compare SFRs measured in multiple bands. Specifically, UV SFR tracers are crucial for galaxies with extended UV disks as well as for faint dwarf galaxies. The first case is that of galaxies forming OB stars in their outskirts, so in conditions of low SFR density wherein H $\alpha$  might be an insufficient SF indicator (Lee J.C. et al. 2009). Whereas, dwarf galaxies have a small dust content thus a lack of extinction effects, which translates in an expected better accuracy of the UV flux than the IR luminosity as a SF tracer.

### 1.5 RADIO CONTINUUM – INFRARED CORRELATION

Massive stars are responsible for most of the far-infrared (FIR) luminosity of a galaxy, attributed to the dust extinction of their emitted UV-visible light, and they also produce most of the RC emission, as the SNRs cause synchrotron radiation. Therefore, the recent SF activity is well traced in these bands and a tight, ubiquitous correlation was found between the global FIR (predominantly non-thermal) and the radio luminosity of normal galaxies (Figure 2) (Condon 1992). Low massive galaxies or those with low SFRs may suffer from deviations from this correlation (Helou et al. 1985).

The slope of this correlation depends on different factors, including the galaxy IR luminosity, the frequency range and the non-thermal to thermal radio emission (Bell E.F. 2003). Samples dominated by faint galaxies ( $L_{IR} < 10^{10} L_{\odot}$ ) tend to have steep radio - IR correlations; instead, for highly luminous galaxies ( $L_{IR} > 10^{10} L_{\odot}$ ) the slopes are close to unity (Yun et al. 2001). This has been interpreted as in low luminous galaxies there is a larger contribution of old stellar populations heating dust to IR luminosity. Also, at low radio frequencies (< 5 GHz) the radio - IR slope is steeper than at higher frequencies due to a higher synchrotron fraction of the radio emission (Price & Duric 1992). Furthermore, the thermal radio continuum, directly tracing SF activity, correlates linearly with the IR luminosity whereas, non-thermal radio emission nonlinearly relates to SF (Bell E.F. 2003).

However, according to (Bell E.F. 2003), there is another important factor that needs to be included in such a framework: the effects of dust opacity. In fact, in highly luminous galaxies the dust is optically thick to FUV light ( $TIR/FUV \gg 1$ ) (Buat et al. 2002), hence, the IR emission is a plausibly good tracer of ongoing star formation activities. Instead, in low-luminosity galaxies the dust is optically thin to FUV ( $TIR/FUV < 1$ ), which implies that the IR emission underestimates the SFR substantially (Wang & Heckman 1996).

If the RC emission in faint galaxies is considered as a good SF tracer while IR emission is clearly not for the aforementioned reasons, then the radio-IR correlation should not be linear. However, it was still found to be more or less linear (e.g., Yun et al. 2001) implying that non-thermal radio emission in low luminosity galaxies must be suppressed. The most likely accepted explanation is that CRes escape from the galaxy due to their small sizes (Chi & Szabelski 1992).

Thus, the linearity of the radio-IR correlation is a conspiracy: both indicators underestimate the SF rate at low luminosities in coincidentally quite similar ways.

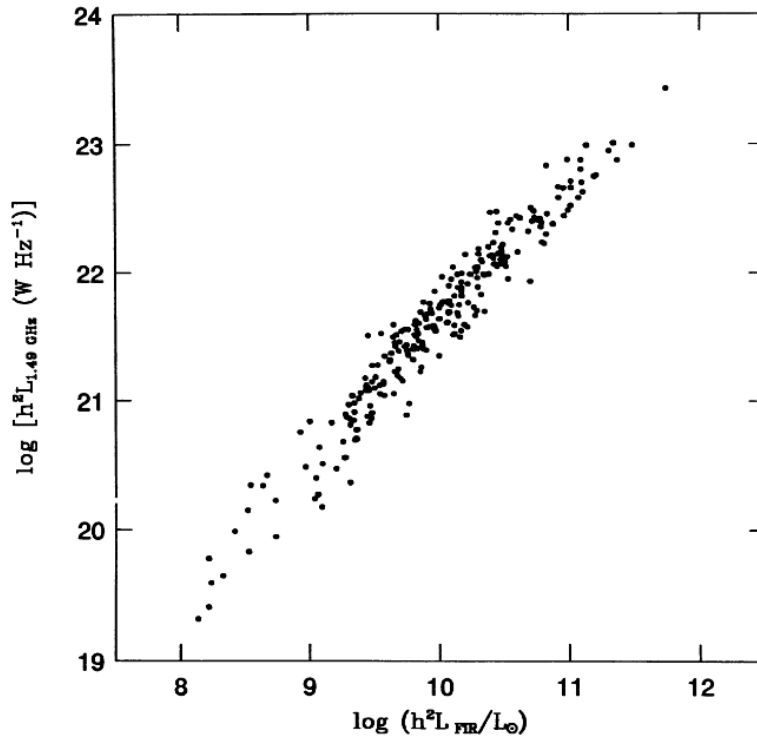


Figure 2: FIR-Radio correlation for star forming galaxies, corresponding to *Figure 8* in Condon et al. 1992. The FIR observations refer to a wavelength of  $\lambda = 60 \mu\text{m}$  whereas the radio observations to a frequency of 1.48 GHz.

## CHAPTER 2: DATA

### 2.1 APERTIF

For the purpose of conducting a star formation analysis of the chosen galaxy sample, I took data provided by the state of the art new generation observing system, Apertif, installed on the Westerbork Synthesis Radio Telescope (WSRT) (Adams E.A.K. et al. 2022).

- In particular, Apertif HI survey (van Cappellen W. A. et al. 2021) provides useful information of the HI emission as well as the kinematics for nearby sources. In addition, the HI measurement also gives a redshift and hence distance to the galaxy. With an improved sensitivity, Apertif aims at characterising and better constraining gas accretion hence galaxy evolution as one of its key science cases (Adams E.A.K. et al. 2022). Another main goal of Apertif HI survey is to detect the smallest gas-rich nearby galaxies that could reveal significant clues on early galaxy formation.

In this study, I used a HI catalog of 1235 objects produced by K. Hess (priv. comm.). This comes from 4.5 months of data (mid-August - 31 December 2019).

- Furthermore, Apertif is also designed to investigate the star formation of radio faint, nearby, galaxies. Specifically, Apertif **DR1** survey is a collection of 249,672 radio sources organised in 3074 radio continuum images, created at a central frequency of 1355 MHz (Kutkin A. M. et al. 2022). The radio continuum catalog covers one year of observing, 1 July 2019 - 30 June 2020; but it has a requirement on data quality so that only a fraction of images (3374) is available.

When studying SF in galaxies, usually SF indicators in different bands of the electromagnetic spectrum are compared as a test of their individual reliability. And especially, having RC data of star forming galaxies calls for their counterparts in the IR window.

### 2.2 WISE

The WISE angular resolution is suitable for providing a sensitive all-sky survey in the mid-infrared with a great variety of targets including brown dwarfs, ultra-luminous galaxies, nearby galaxies, AGNs, interstellar dust and young stars (and many more) (Wright et al. 2010).

The WISE telescope has a high sensitivity spectral response in four main infrared bands: W1 at  $3.4 \mu m$ , W2 at  $4.6 \mu m$ , W3 at  $12 \mu m$  and W4 at  $22 \mu m$ . The two near-infrared (NIR) bands, W1 and W2, are particularly efficient to track the emission from evolved stars and the galactic interstellar medium hence, they are widely used to measure galaxy stellar masses and the mass-to-light-ratio ( $M/L$ ), where  $M$  is the galaxy stellar mass while  $L$  its luminosity (Jarrett et al. 2023). Whereas, at MIR and FIR ranges, W3 captures both atomic and molecular lines and continuum emission and W4 is sensitive to the small-grain dust continuum from star formation processes (Jarrett et al. 2013). Therefore, W3 and W4 are the most appropriate to track SF activity in galaxies.

A very comprehensive catalog for the infrared photometry of galaxies is **ALLWISE** (Cutri et al. 2013). This provides information for a number of 747,634,026 sources at all WISE bands.

The **WISE Extended Source Catalogue (WXSC)** comprises more accurate measurements of fluxes for nearby galaxies, as explained in (Jarrett et al. 2019). At very low redshifts, galaxies are likely resolved at  $3.4 \mu\text{m}$ , however contaminations may occur during the extraction of photometry. Therefore, an important point of improvement by WXSC is the new total flux in the W1 band (as well as other colors) as a fundamental tracer of the stellar masses. In fact, thanks to the advanced W1 luminosity and colors, more accurate stellar-mass scaling relations were derived with better than 25-30% accuracy in more massive regimes while  $< 40\text{-}50\%$  for  $M < 10^9 M_{\odot}$  (Jarrett et al. 2023).

### 2.2.1 ALLWISE VS WXCS

In Figure 3, I show a comparison of W1 fluxes derived in the same way as the WXSC (T. Jarrett, priv. comm.) to those in ALLWISE for my galaxy sample, selected as described in subsection 3.1. Since WXSC has improved accuracy than the earlier ALLWISE, I decided to use its new optimized data for further calculations in scope for this study.

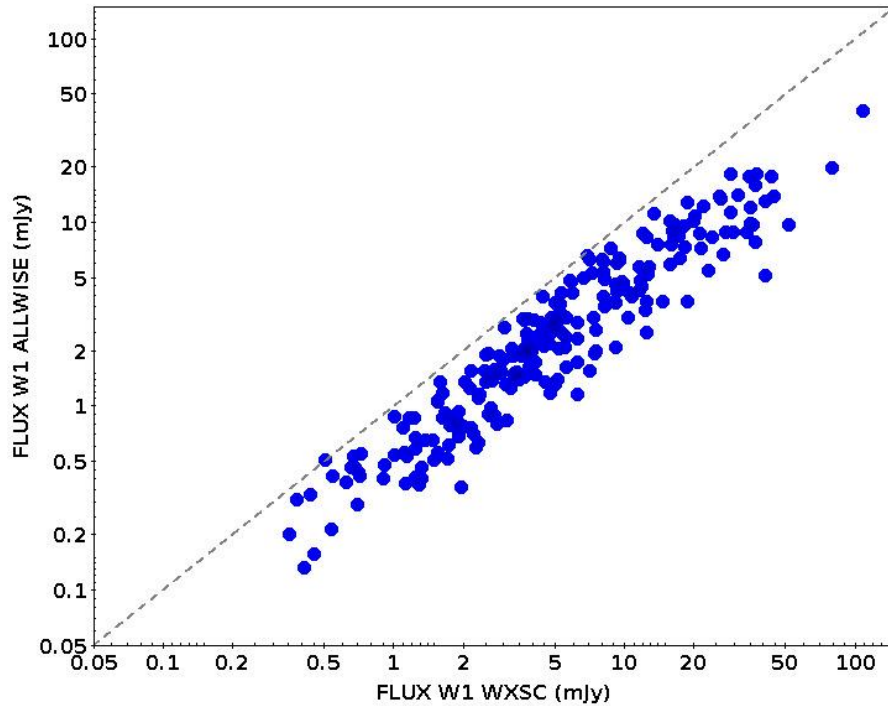


Figure 3: Comparison of W1 fluxes in WXSC and ALLWISE. The black dashed line is a one to one line for reference.

## 2.3 GALEX

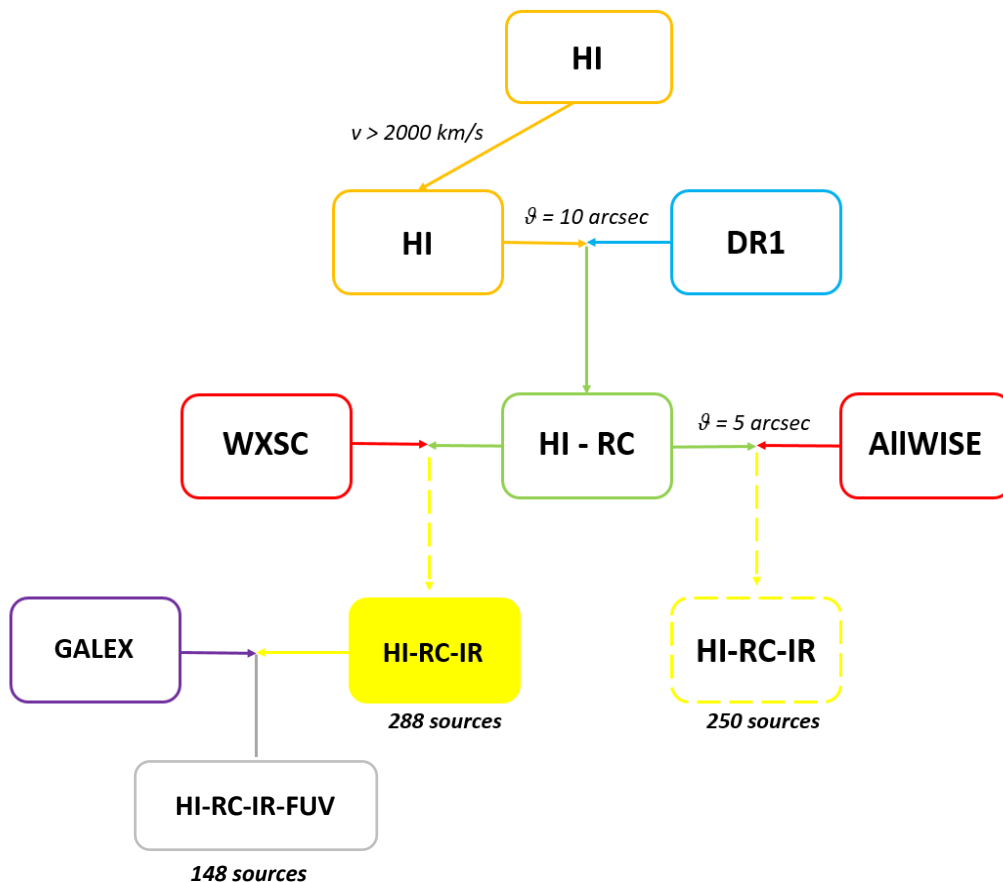
The most direct tracer of recent SF activity comes from the young massive starlight in the UV range. In this spectral window, the Galaxy Evolution Explorer (GALEX) provides a series of sky surveys with measurements in two bands: FUV (Far Ultraviolet) with a central wavelength of  $\lambda_{mean} = 1528 \text{ \AA}$  and NUV (Near Ultraviolet) with  $\lambda_{mean} = 2310 \text{ \AA}$  (Bianchi et al. 2017).

These have really given an important contribution to the studies of hot stellar objects, star forming galaxies as well as the interstellar medium. The measured sources in the current GALEX database (data release **GR6 + 7**) are around 82,992,086 most of which well characterised in photometry at the two bands. In particular, GALEX photometry is optimised for point sources, whereas for extended sources it might result in underestimated flux densities (Burgarella et al. 2020).

## CHAPTER 3: METHODOLOGY

### 3.1 GALAXY SAMPLE

In this section, I show how I built my galaxy sample. First, I collect all the steps in a schema then, I describe each precisely.



- Since I performed an analysis of star formation activity in galaxies, I needed sources with a proper gas content. This requirement is essential to find star-forming galaxies and avoid other sources i.e. AGNs. Therefore, I started from taking objects in Apertif HI catalog (K.Hess, priv. comm.) that includes data of their HI emission as well as their redshift, hence distance, crucial for the measurements of this work.

I filtered data considering only galaxies with  $v_{sys} > 2000 \text{ km/s}$  to exclude very nearby galaxies, as their peculiar motion could result in an under- or over- estimated luminosity distance,  $D_L = v_{sys}/H_0$ . In the end, I obtained a list of selected 1089 galaxies.

- For the purpose of studying different SFR tracers, I required these objects to also have RC emission. Therefore, I have cross-matched the selected sample of Apertif HI catalog, with Apertif DR1 catalog. In doing so, I have used an angular distance of 10 arcseconds that, from a histogram of statistics (Figure 4), has resulted in an optimal choice to include a significant number of best-matched galaxies. This cross matching has produced a sample of 288 galaxies with detected HI and RC emission. Apertif beam size is 15 arcseconds (or larger), but the centroiding accuracy can be much higher than that. However, the considered sources are extended and could have different morphologies between radio continuum and HI. Therefore, even if the centers could be known with a much higher accuracy, they could be different because galaxies have different shapes.
- Furthermore, I cross-matched the list of 288 galaxies with the ALLWISE catalog (Cutri et al. 2013). This time I used a separation of 5 arcseconds, as the resolution of WISE is much higher than Apertif's. This step produced a catalog of 250 best-matched sources with HI, RC emission by Apertif and IR data by ALLWISE. Specifically, I used this sample to compare ALLWISE with optimized IR data of the WXSC.
- T. Jarrett (priv. comm.) provided me with IR improved extended source photometry (WXSC) for all the 288 galaxies selected by cross-matching Apertif HI and DR1 catalogs.

### 3.1.1 FUV-IR-RC DATA

To further study the consistency of SFR tracers in the IR and radio bands, I also compared them with the FUV-derived ones. Therefore, in a later step of my analysis, I built a galaxy sample out of the cross matching between the list of 288 galaxies, described above, and *GALEX GUV\_cat\_AIS GR6 + 7* catalog (Bianchi 2017). I used a matching distance of 8 arcseconds that, from a histogram of statistics, has resulted in a good choice to keep a high rate of sources in the sample, 178 best - matched objects. However, 30 sources do not have FUV fluxes measured by GALEX, while the NUV are available. The FUV is considered more reliable in tracing the recent star formation, unlike the NUV wavelengths which trace a major contribution from stars with lifetimes  $> 100 \text{ Myrs}$ . Therefore, in this final phase, I used a sample of 148 sources for which I had information in all the desired bands (RC, IR, FUV).

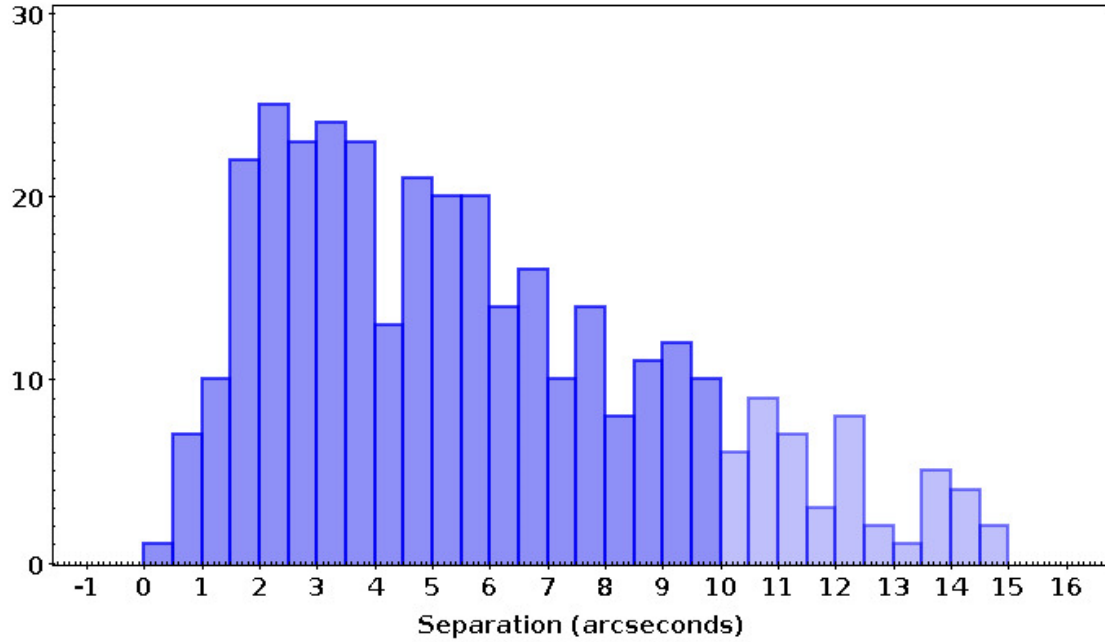


Figure 4. Histogram of statistics for the choice of the tolerance (arcseconds) in cross-matching HI and DR1 Apertif catalogs. The selected tolerance is 10 arcseconds.

### 3.2 STAR FORMATION RATE CALCULATIONS

As a result of the available SFR tracers and the initial assumptions made (IMF, metallicity and star formation history<sup>1</sup>), there can be different calibrated relations to get the SFR from the galaxy luminosities at specific wavelengths. The calibration coefficients of the formulas change depending on the initial conditions (i.e. IMF and metallicity) assumed for the galaxy sample.

#### **IR SFRs**

One extensively used equation from the literature is connected to the  $L_{TIR}$  (Calzetti 2012), from which the SFR can be derived as:

$$SFR \left( \frac{M_{\odot}}{yr} \right) = 2.8 \times 10^{-44} \times L_{TIR} (erg s^{-1}) \quad (1)$$

<sup>1</sup> The star formation history tells how star formations occurs over time and space, whether in short bursts or over longer periods.



This expression holds for a Kroupa IMF, Starburst99 (Leitherer et al. 1999) models assuming solar metallicity and a constant star formation over  $\tau = 100 \text{ Myr}$ .

However, (Cluver et al. 2017) showed that the IR luminosity at specific bands,  $12 \mu\text{m}$  and  $22 \mu\text{m}$ , corresponding to W3 and W4 WISE bands, respectively, well relate to the  $L_{TIR}$  and therefore could be used as monochromatic luminosities to derive directly the SFRs (equation 4 and equation 5 in Cluver et al. 2017).

In this study, I used the IR SFRs provided in the WXSC catalog. In addition to the SFRs based on the W3 and W4 WISE band fluxes ( $SFR_{W3}$ ,  $SFR_{W4}$ ), there are also  $SFR_{mir}$ , derived from a combination of the two as well as a corrected value,  $SFR_{mircor}$  (Cluver et al., in preparation). The latter uses a FUV normalization that takes into account for the intrinsically lower IR SFR of low mass galaxies, as a consequence of their lower dust content compared to more massive regimes.

### **RADIO SFRs**

A calibrated relation for RC-based SFRs is that of (Condon 2002), also followed by i.e. Heesen et al. 2014 and Cluver et al. 2017, to derive SFRs at a central wavelength of  $\sim 22 \text{ cm}$ . This expression is in the form:

$$SFR_{RC} \left( \frac{M_{\odot}}{\text{yr}} \right) = 0.75 \times 10^{-21} \times L_{1.4\text{GHz}} (W \text{ Hz}^{-1}) \quad (2)$$

I employed equation (2), with radio luminosities normalized to the reference frequency of 1355 MHz, to measure the RC SFRs of my 288 galaxies.

### **UV SFRs**

To convert the FUV fluxes I took from GALEX into UV-SFRs, I used the calibrated expression in equation 3 of (Lee C. et al, 2009) in the form:

$$SFR_{UV} \left( \frac{M_{\odot}}{\text{yr}} \right) = 1.4 \times 10^{-28} \times L_{FUV} (erg \text{ s}^{-1} \text{ Hz}^{-1}) \quad (3)$$

As already mentioned, the FUV better traces the recent SF activity.

### 3.3 VISUAL INSPECTION

A crucial step I performed before analyzing the SFR trends is the visual inspection. This is because my galaxy sample might be contaminated by background sources or AGNs lying in the same field of view as well as affected by other interference (i.e. by stars....).

In this analysis, I overplotted RC contours on ALLWISE images (using the W1 band) for the 288 sources described above; some examples are presented in this subsection while all figures are shown in Appendix. I individuated four classes of objects:

1. Good data is the best collection of objects, whose RC contours perfectly follow the disk of the galaxy, which means that clearly IR and RC are tracing SF. Moreover, in this class there are also objects with RC contours concentrated in a specific part of the galaxy as I considered that SF could occur in a particular location. Some examples are shown in Figure 5. With this class of objects I produced a "clean sample" of 156 sources that I will use in my SFR trends.
2. The second class is that of objects with radio contamination from other sources, which is seen when RC contours are much bigger than the galaxy shape or when they are blended. Some examples are shown in Figure 5.
3. The third class is that of sources contaminated by others in the WISE images. To support my WISE contaminated choices I show also the corresponding images of the WXSC, provided by T. Jarrett (priv. comm.). Here contaminating sources are masked but the uncertainty still remains. Some examples are shown in Figure 6.
4. The last class contains data with a bad match of WISE and RC. The inconsistency is visible as they appear like be tracing different objects. Some examples are shown in Figure 6.

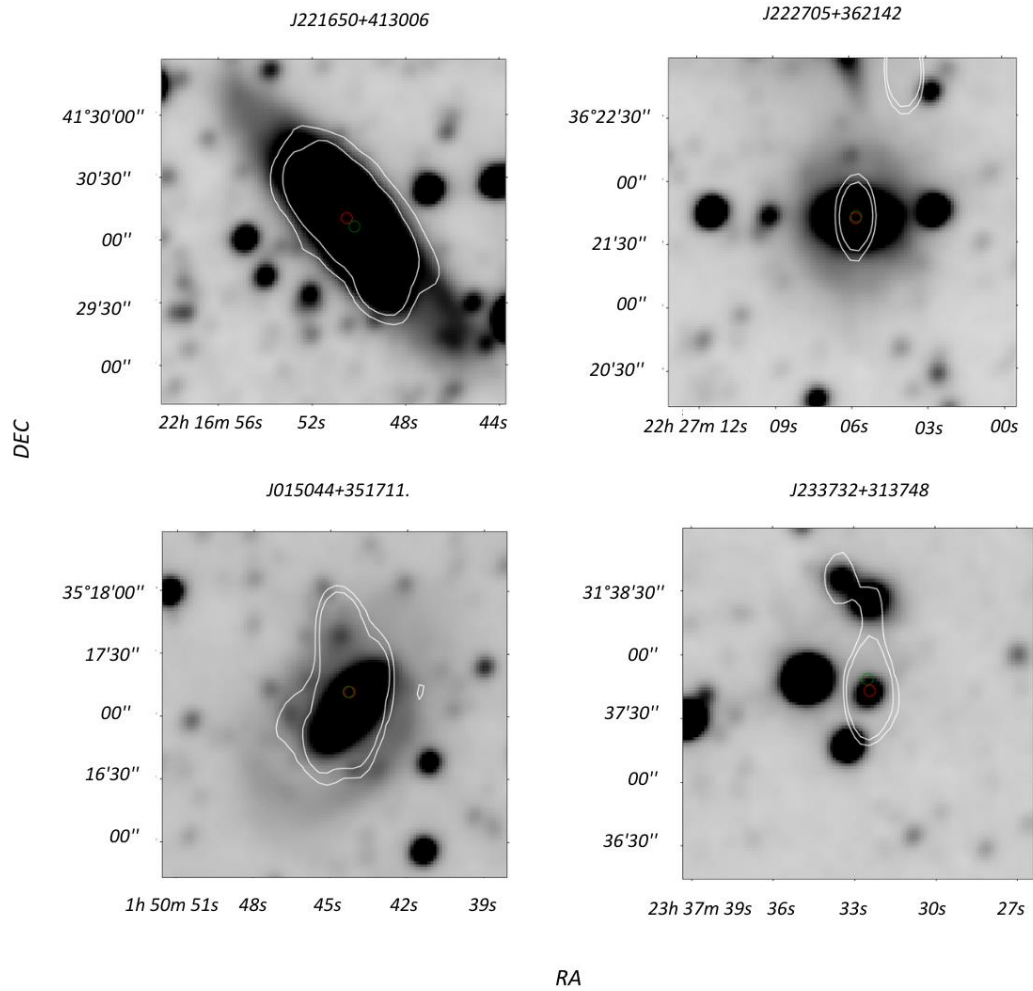


Figure 5: Top panel: two examples of good data; on the left a perfect match of radio contours with the shape of the galaxy in the WISE image whereas on the right an example of radio contours concentrated in a specific part of the galaxy. Bottom panel: two examples of radio contamination with radio contours that extend to other sources. The green and red circles are the centers of the source in WISE and RC images respectively.

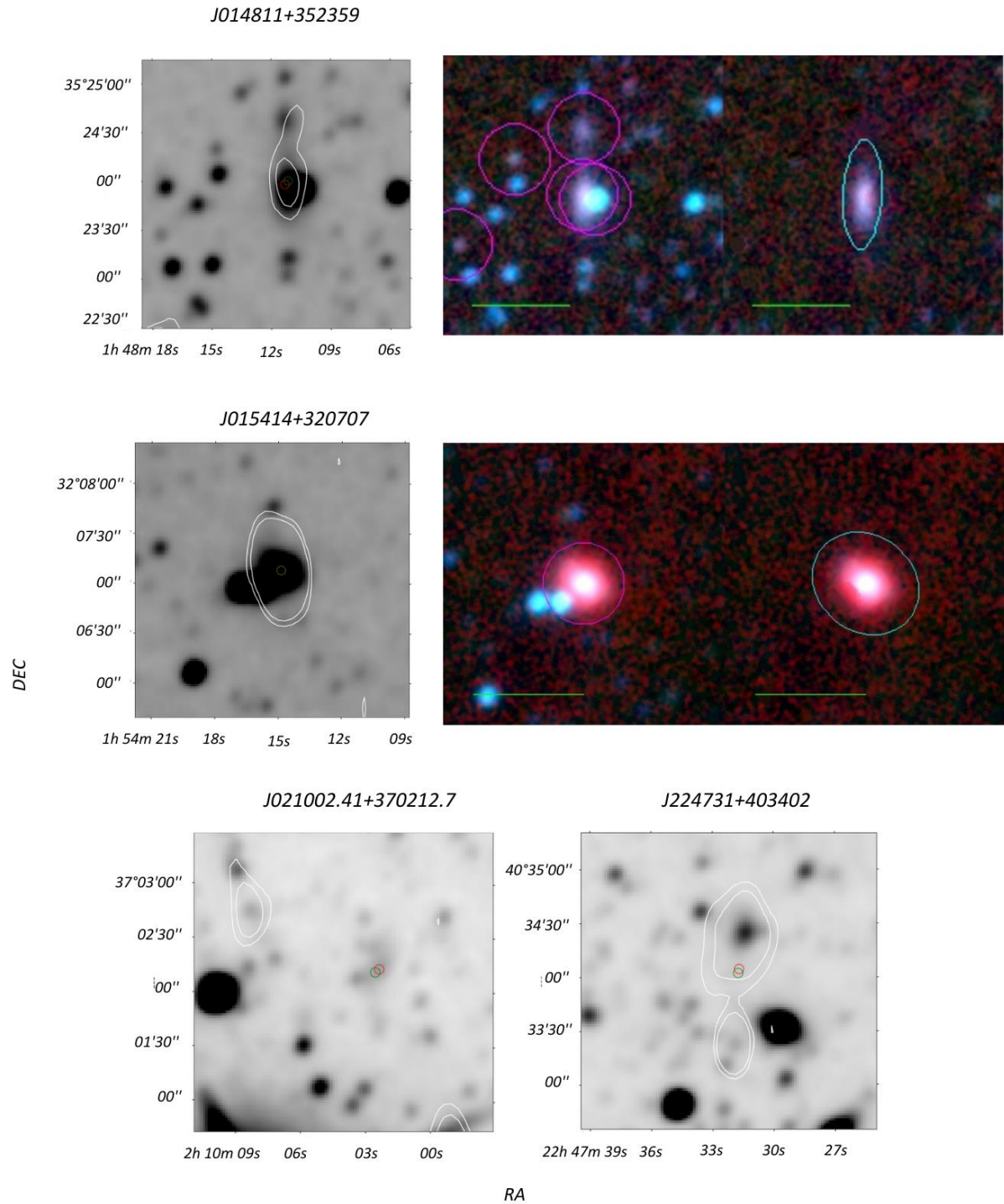


Figure 6. First two panels: examples of WISE contaminated data seen in both ALLWISE images and the corresponding images provided by T. Jarrett (priv. comm.). In the latter, contaminating sources are masked. Bottom panel: two examples of bad data where the RC and WISE do not trace a clear source and are not matched with each other. The green and red circles are the centers of the source in WISE and RC images respectively.

## CHAPTER 4: RESULTS

### 4.1 NUMBER OF DWARF GALAXIES IN THE SAMPLE

In this step, in addition to calculating stellar masses, I explored the improvements of WXSC with respect to ALLWISE. In doing so, I compared the stellar masses of my galaxy sample, provided as WXSC data, with the ones I calculated using the W1 flux from ALLWISE.

I followed the approach described in (Jarrett et al. 2023) and reported below, to measure the stellar masses ( $M$ ) of all the 250 sources of which I have ALLWISE information.

$$M_{abs} = M_{W1} - 5 \text{Log} \left( \frac{D_L(pc)}{10} \right) \quad (4)$$

$$L_{W1} = 10^{-0.4(M_{abs} - M_{sun})} \quad (5)$$

$$\text{Log } M = A_0 + A_1(\text{Log } L_{W1}) + A_2(\text{Log } L_{W1})^2 + A_3(\text{Log } L_{W1})^3 \quad (6)$$

Where:  $A_0 = -12.62185$ ,  $A_1 = 5.00155$ ,  $A_2 = -0.43857$ ,  $A_3 = 0.01593$

Equation (6) shows how to estimate the stellar mass of galaxies if their infrared luminosity in the W1 band ( $L_{W1}$ ) is known. The WISE W1 band, is particularly appropriate to estimate the global stellar mass of galaxies as, in that window, the luminosity is dominated by the evolved stellar populations, low mass stars that give the most significant contribution to the overall galaxy mass as they are very numerous (Jarrett et al. 2023). In equation (4)  $M_{abs}$  and  $M_{W1}$  are the absolute magnitude and the apparent magnitude in W1 band of each source, respectively, and  $D_L(pc)$  the luminosity distance in parsecs. In equation (5)  $M_{sun}$  is the absolute magnitude of the Sun in the W1 band and its value is 3.24 mag (Jarrett et al. 2013).

These calculations, based on ALLWISE, have resulted in 37 found galaxies with stellar mass  $\leq 10^9 M_{\odot}$ , which I initially thought to be a fair number of dwarf galaxies (37/250) to explore. However, when improved WXSC data was available, only 9 of them survived in this low mass range, implying that ALLWISE had underestimated luminosity and thus galaxies were more massive than previously found.

## 4.2 STELLAR MASS VS SFR

In this section, I use the SFR derived from the WISE W3 band as well as the MIR data ( $sSFR_{mir}$ ,  $sSFR_{mircor}$ ) to explore their relation with the stellar masses of galaxies.

In particular, in the top panel plots of Figure 7, I compare my data to that studied by Cluver et al. 2017. Since the clean sample I am using has revealed not to include galaxies with a mass smaller than  $10^9 M_{\odot}$ , I can only test the consistency of this comparison at higher mass regimes.

In the top left plot, while the clean sample shows a more compact trend of more massive objects forming more stars, as traced in the W3 band, data points from Cluver et al. 2017 appear to have a more spread distribution with also high mass galaxies having smaller SFRs than less massive ones. Overall, there is an agreement of data in the mass range  $10^9 M_{\odot} < M < 10^{12} M_{\odot}$ .

I also use the same study of Cluver et al. 2017 as a reference sample to investigate the relation between the specific SFR at W3 ( $sSFR_{W3}$ ), which is the SFR per unit mass, and the stellar mass of galaxies. This is shown in the top right panel of Figure 7 and again there is a reasonable agreement between the two different samples in the mass range said before. However, in the sample of Cluver et al. 2017 there are more galaxies with a higher sSFR compared to those in the clean sample of this study, due to their broader mass range.

Whereas, in the bottom panel plots, I investigate the difference between the full sample and the clean sample through the relation between the  $sSFR_{mir}$ , &  $sSFR_{mircor}$  with the stellar masses. Here a clear trend appears showing that low mass galaxies are forming relatively more stars per unit mass than the more massive ones. This is especially visible when using the corrected MIR values and it is a consequence of the FUV calibration that accounts for the lower dust content in small galaxies. This method, in fact, appears to have a significant impact only at smaller regimes.

However, the very small objects are excluded from the clean sample after the visual inspection.

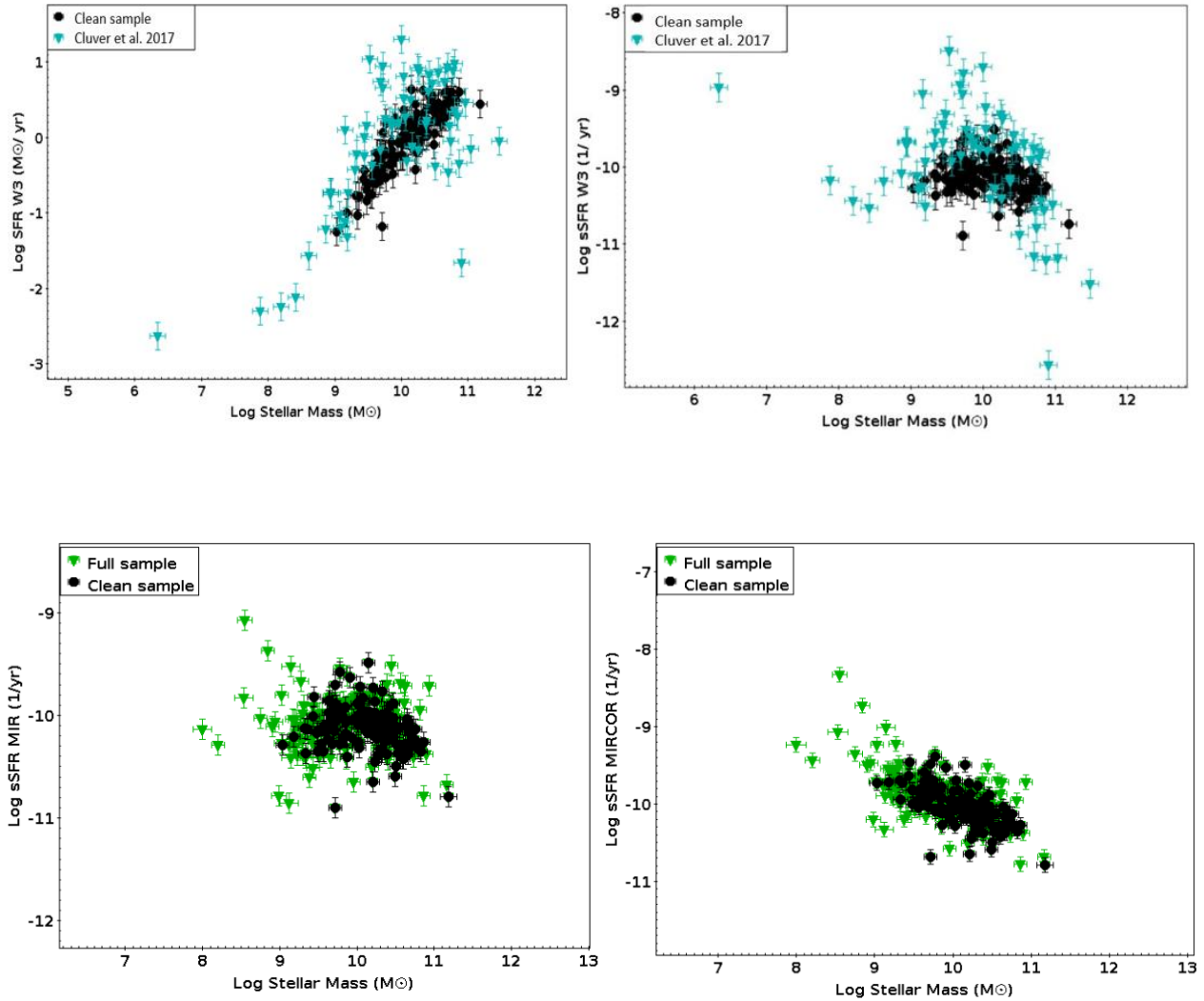


Figure 7. Top panel plots:  $\log SFR_{W3}$  and  $\log sSFR_{W3}$  vs  $\log$  stellar mass, from left to right respectively. The cyan data points correspond to the sample studied by Cluver et al. 2017. The black data points belong to the clean sample of this study. Bottom panels: the left plot shows the  $\log sSFR_{mir}$  vs  $\log$  stellar mass while the right one the relation between the  $sSFR_{mircor}$  vs  $\log$  stellar mass. The black points belong to the clean sample, the green data points to the full sample.

### 4.3 IR vs RC SFR

Here I present the correlation between the IR derived SFRs at the WISE W3 and W4 bands with the RC based one ( $SFR_{RC}$ ). I first show, in Figure 8, the three subclasses I created in the visual inspection process, the clean sample, the WISE contaminated and RC contaminated objects. The radio and WISE contaminated objects do not occupy different regions, instead, they are spread similarly all over the distribution. This suggests that radio contamination adds extra radio flux, increasing RC SFRs. On the other hand, the mask of contaminating sources in WISE images results in artificially lower measured fluxes thus lower IR SFRs.

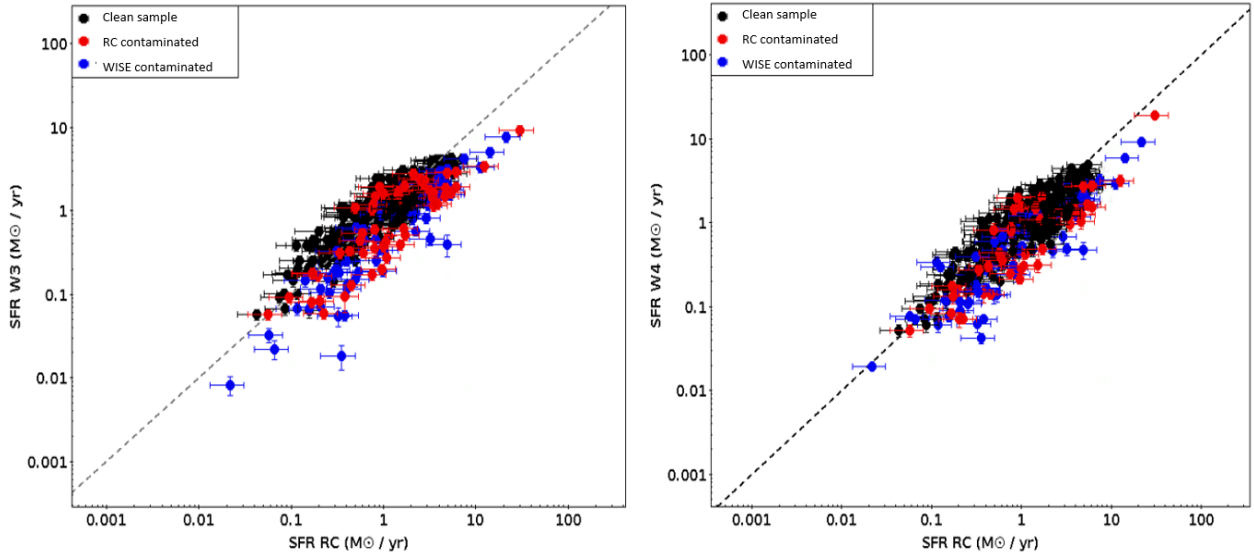


Figure 8: Plots of the  $SFR_{W3}$  vs  $SFR_{RC}$  and  $SFR_{W4}$  vs  $SFR_{RC}$  from left to right respectively. The black data points belong to the clean galaxy sample, the red ones to RC contaminations and the blue to WISE contaminations. The dashed gray line is a one to one relation for reference.

In the following plots, in Figure 9, I analyse the correlations between  $SFR_{W3}$  &  $SFR_{W4}$  with  $SFR_{RC}$  from left to right, respectively. Here, I compare the trends of the clean sample of this study with the one investigated in Cluver et al. 2017. The distributions of the two different studies look consistent. In particular, the slope of the best fit I found for  $SFR_{W3}$  vs  $SFR_{RC}$  ( $0.847 \pm 0.015$ ) is plausibly close to 1 and similar to that in Cluver et al. 2017 (Figure 13 a), as compared in Table 1. Data points of the clean sample are well correlated, as suggested by the Pearson correlation coefficients of 0.94, meaning that, therefore, the linear relation well describes the distribution. The estimated offset to the best fit is 0.13 consistent with that of the reference sample.

The  $SFR_{W4}$  and  $SFR_{RC}$  show an even better linear correlation of data points as suggested by the bigger Pearson correlation coefficient of 0.98. This linear relation has a slope of ( $0.881 \pm 0.019$ ), plausibly close to 1 and consistent with that of the reference sample in Cluver et al. 2017 (Figure 13 b), as compared in Table 1. The estimated offset to the best fit is 0.12, consistent with that of the reference sample.



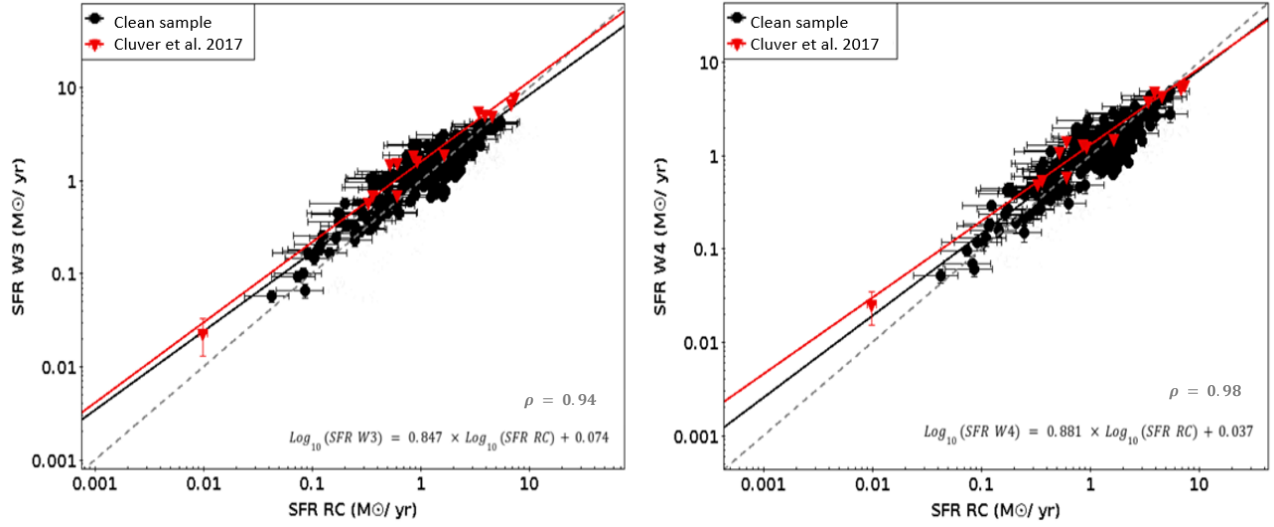


Figure 9: Plots of the  $SFR_{W3}$  vs  $SFR_{RC}$  and  $SFR_{W4}$  vs  $SFR_{RC}$  from left to right respectively. The red data points and fit are taken from Cluver et al. 2017. The black data points and fit, for which I give the expression, and the correlation factor belong to the clean galaxy sample. The dashed gray line is a one to one relation for reference.

Table 1: Best fits of the clean sample of this study and the reference sample of Cluver et al. 2017

	$SFR_{W3}$ VS $SFR_{RC}$	$SFR_{W4}$ VS $SFR_{RC}$
<b>CLUVER ET AL 2017</b>	$Log_{10}(SFR W3) = 0.842 \times Log_{10}(SFR RC) + 0.21 \pm 0.072$ $\pm 0.04$	$Log_{10}(SFR W4) = 0.845 \times Log_{10}(SFR RC) + 0.12 \pm 0.087$ $\pm 0.05$
<b>CLEAN SAMPLE</b>	$Log_{10}(SFR W3) = 0.847 \times Log_{10}(SFR RC) + 0.074 \pm 0.015$ $\pm 0.08$	$Log_{10}(SFR W4) = 0.881 \times Log_{10}(SFR RC) + 0.037 \pm 0.019$ $\pm 0.06$

I now analyze how the IR SFRs corrected using FUV values ( $SFR_{mircor}$ ) correlate to  $SFR_{RC}$ . In particular, in the plot in Figure 10, I visualize both the clean and full samples to better understand the effect of this normalization. Clearly, the major impact of the correction is on the smaller SFR measurements, typical of lower mass galaxies, which increase significantly. Therefore, when considering that the IR tracers (at W3 and W4) might be underestimating SFRs due to the lower dust extinction in small sources, the trend deviates dramatically from the one to one line in the left end. The slope of the fit for the clean sample is  $0.631 \pm 0.010$ .

As expected, the FUV normalization works at the low mass regimes but it has a very little or no effect at the intermediate/higher ones. The main idea is that the dust amount and opacity of fainter objects are insufficient in absorbing the UV light of newborn stars and re-emitting that into the IR range.

Overall, data points look closely distributed along the linear fit, as suggested by the Pearson correlation coefficient of 0.94 and the estimated offset of 0.10.

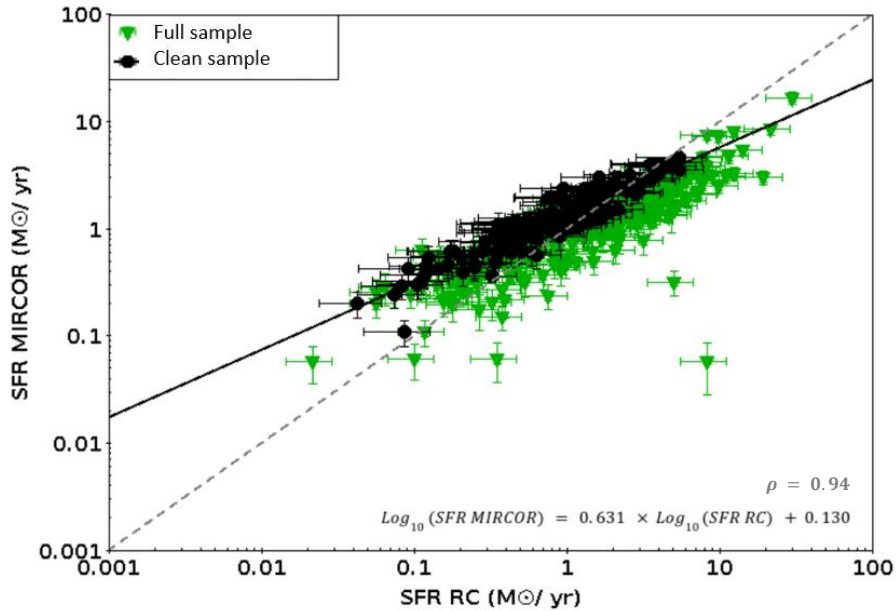


Figure 10: Plot of the  $SFR_{mircor}$  vs  $SFR_{RC}$ . The green data points represent the initial complete sample. The black data points and the fit, for which I give the expression, and the correlation factor refer to sources of the clean galaxy sample. The dashed black line is a one to one relation for reference.

#### 4.4 IR vs FUV SFR

In Figure 11, I show the relations between IR SFRs ( $SFR_{W3}, SFR_{W4}$ ) with the FUV derived ones ( $SFR_{FUV}$ ), comparing the behavior of the clean and the full samples. In both plots, the distributions of data points appear very scattered. For the clean sample, this is also suggested by the estimated offsets to the best fits of 0.35 and 0.36 respectively. The linear correlations of data points are not strong as suggested by the Pearson correlation coefficients, of 0.51 and 0.49 respectively. The found linear fits deviate totally from the one to one line.

At small SFRs the W3 and W4 appear to measure more SF than the FUV, contrary to the expectations. In fact, smaller values should be better traced by the FUV for the reason explained in the previous paragraph. The possible reason for the very big discrepancy might be that FUV tracer is affected by dust or FUV data are not very accurate.

In Figure 12, I present the relation between  $SFR_{mircor}$  and  $SFR_{FUV}$  for the full and clean samples. The FUV normalization makes data points increase at lower values. In this case, the scatter is less than with the previous IR tracers (W3, W4) and, for the clean sample, this is also suggested by the smaller offset to the best fit, of 0.25. Also in this case, the linear correlation is not very strong as suggested by the Pearson coefficient (0.48).

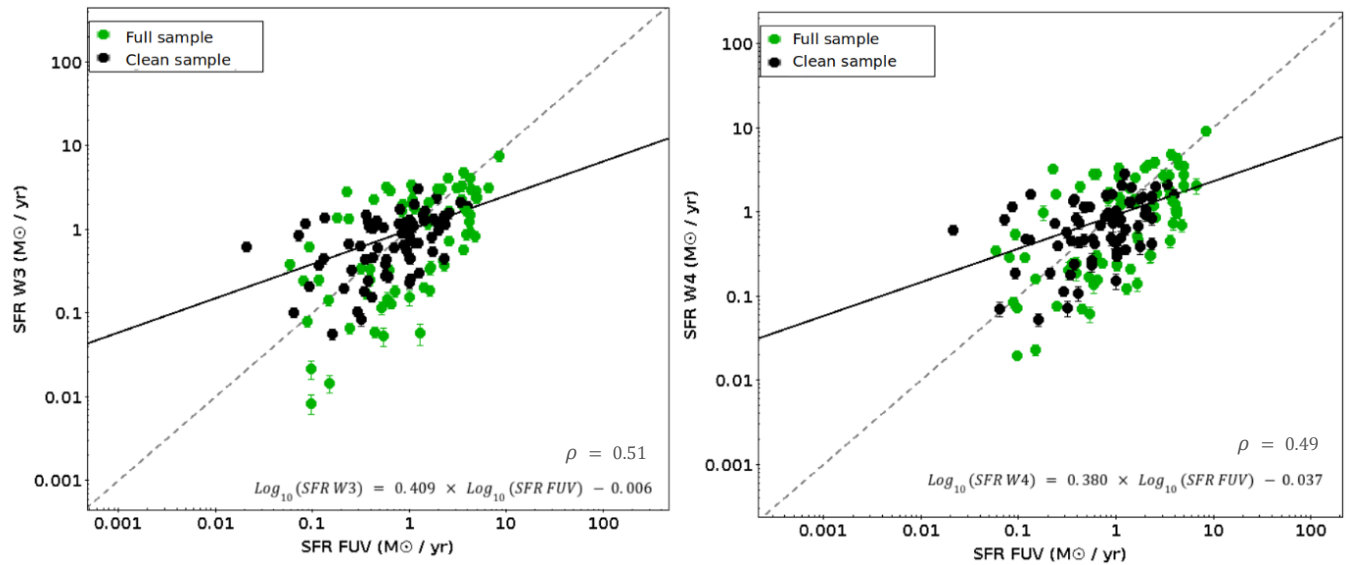


Figure 11: In the left panel is the plot of  $SFR_{W3}$  vs  $SFR_{FUV}$  while in the right panel of  $SFR_{W4}$  vs  $SFR_{FUV}$ . The green data points represent the initial complete sample. The black data points and the fit, for which I give the expression, and the correlation factor refer to sources of the clean galaxy sample. The dashed black line is a one to one relation for reference.

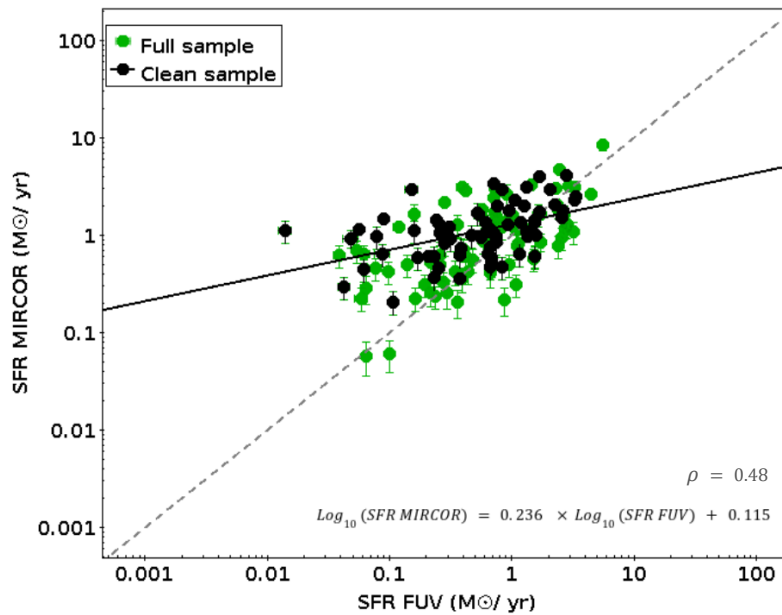


Figure 12: In this panel is the plot of  $SFR_{mircor}$  vs  $SFR_{FUV}$ , the green data points represent the complete sample. The black data points and the fit, for which I give the expression, and the correlation factor refer to sources of the clean galaxy sample. The dashed black line is a one to one relation for reference.

#### 4.5 RC vs FUV SFR

In this last section of results, I present the relation between  $SFR_{FUV}$  and  $SFR_{RC}$  (Figure 13) for both the full and the clean samples.

Here, data points have less vertical scatter than in the case of correlations between IR SFRs at W3 and W4 vs  $SFR_{FUV}$  (Figure 11). This is suggested by the offset to the best fit of 0.33. Still the linear fit is far from the one to one line, with a slope of  $0.473 \pm 0.113$ . The overall trend shows that  $SFR_{RC} > SFR_{FUV}$  in both samples, with a very few data points well related (on the one to one line). Also in this case, the discrepancy of the two tracers is clear; the RC based SFR might be more reliable than the FUV counterpart as the latter is affected by dust extinction while the radio band is not.

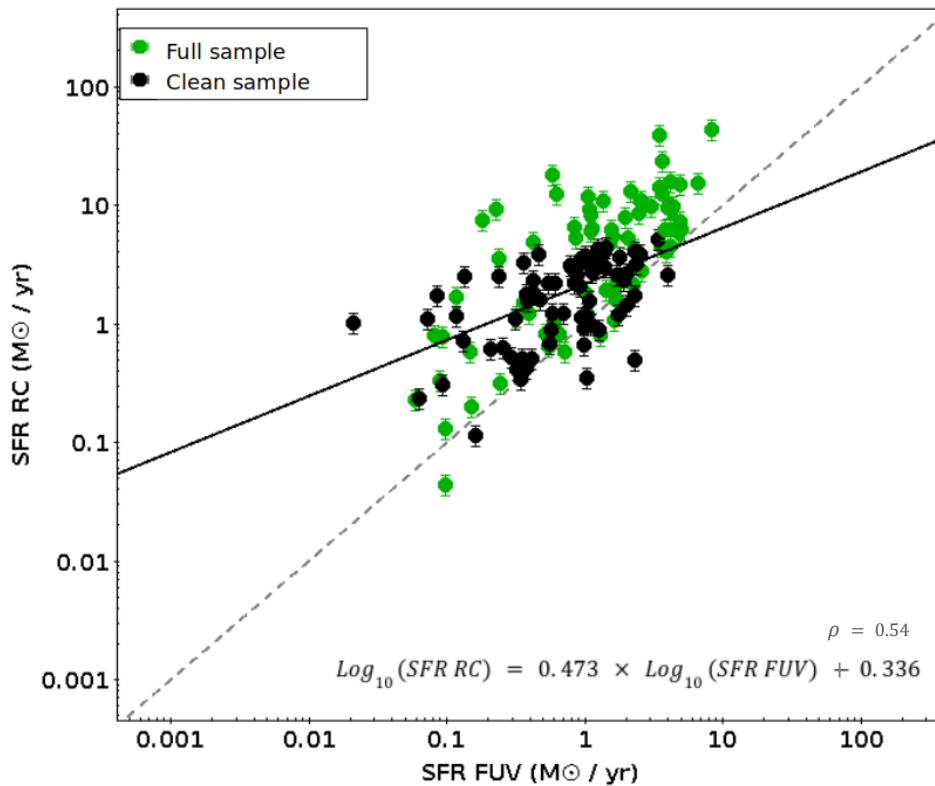


Figure 13: Plot of the  $SFR_{FUV}$  vs  $SFR_{RC}$ . The green data points represent the complete sample. The black data points and the fit, for which I give the expression, and the correlation factor refer to sources of the clean galaxy sample. The dashed black line is a one to one relation for reference.

## CHAPTER 5: DISCUSSION

### 5.1 LACK OF DWARF GALAXIES IN SAMPLE

The improved WXSC W1 fluxes, good tracers of galaxy stellar masses, as well as the new calibrated mass relations provided in Jarrett et al. 2023, revealed the galaxy sample of this study to be less dwarf dominated than I expected and than I previously found using ALLWISE data. The possible reason for this might be the sample selection itself; requiring both a higher redshift and a radio continuum footprint in galaxies must have excluded the smaller ones, with a fainter radio continuum. In order to include as much dwarf galaxies as possible, this study could be performed starting from different initial conditions, i.e. without the lower distance cutoff or placing requirements for the RC, using improved Apertif data products or larger samples.

### 5.2 CONTAMINATED SOURCES

WISE contaminated sources can be easy to identify, as there are clearly objects that lie on top of the specific source of interest. Sometimes, also faint but very close objects might be considered as contaminating.

Radio contaminations appear with blended or spread RC contours that extend more than the galaxy shape. Occasionally, the radio seems displaced from the selected objects suggesting it is not really tracing SF activity in that source.

RC and WISE contaminated objects, as plotted in Figure 8 ( $SFR_{W3}$  vs  $SFR_{RC}$  &  $SFR_{W4}$  vs  $SFR_{RC}$ ), are spread in the whole distributions of data points, without a clear separation. As anticipated in the previous section, the overlap might be due to the radio contamination adding extra radio flux thus increasing RC SFRs as well as the mask of contaminating sources in WISE images, which results in artificially lower measured fluxes hence, lower IR SFRs.

### 5.3 FIR-RADIO SFR CORRELATIONS

Preliminarily, I explored the relation of IR SFRs with the stellar masses of galaxies. In particular in the plot  $\text{Log } sSFR_{mir}$  vs  $\text{Log}$  stellar mass, in Figure 7, there is a flat distribution of data points. Instead, in the plot  $\text{Log } sSFR_{mircor}$  vs  $\text{Log}$  stellar mass, a small trend appears with lower mass galaxies forming relatively more stars per unit mass than the more massive ones. This suggests that the FUV normalization has a greater impact on low mass galaxies, making their SFRs significantly increase.

As known from the literature (Jarrett et al. 2017), the MIR and FIR WISE W3 and W4 bands are optimal tracers of recent star formation as, unlike W1 and W2, they are not polluted by old stars: W3 captures atomic and molecular lines and continuum emission while W4 is sensitive to the continuum of small dust grains. As shown in section 4.3, these IR monochromatic tracers work well for the clean sample and agree reasonably with the  $SFR_{RC}$ . Additionally, the found correlations are almost consistent with those of Cluver et al. 2017, as shown in the comparing table of the same section. In this work, there is a tight correlation between  $SFR_{W4}$  and  $SFR_{RC}$ . This last good agreement leads to the conclusion that SF is better traced in W4 than in W3. And this suggests that dust extinction has a great impact on the star-forming environment

of the selected sources; therefore, most of the UV light emitted by freshly formed stars is reprocessed by dust and emitted in a frequency range that corresponds to the WISE W4.

However, in the trend  $SFR_{mircor}$  vs  $SFR_{RC}$ , in Figure 10, the good correlation breaks at smaller SFR values. This is a consequence of the FUV normalization that specifically targets low SFRs, typically found in galaxies with a little dust. Data points at small values are thus found prominently above the one to one line whereas, the higher ones remain almost untouched, as they are not impacted by the FUV normalization. This suggests that, on the one hand, both  $SFR_{W3}$  and  $SFR_{W4}$  might be underestimating the smaller SFRs. In fact, at such regimes, IR tracers are questionable on the basis of a lack of copious dust, optically thin and not efficient in absorbing the starlight. In addition, the small size and dust opacity of low mass galaxies could result in a suppressed radio emission (Bell E.F. 2003); the possible reason might be that cosmic ray electrons accelerated by supernovae escape the galaxy before undergoing energy loss (Heesen et al. 2022). On the other hand, the consistency of the FUV normalization should be better tested in a sample dominated by low mass sources.

#### 5.4 COMPARISON WITH FUV SFRS

Given the discrepancy between WISE & RC SFRs the idea was to use FUV as another tracer to see if it could determine which was a better tracer - was  $SFR_{RC}$  under-predicting or  $SFR_{mircor}$  over-predicting at lower SFR values?

In the plot  $SFR_{W3}$  and  $SFR_{W4}$  vs  $SFR_{FUV}$ , in Figure 11, I would have expected a majority of small SFR values in the clean sample to have a higher SFR measured by FUV. They, instead, are very scattered and they have higher IR values. This might be due to limitations related to dust extinction effects as well as to the UV photometric measurements. In fact, GALEX source catalog is point-source optimized, like ALLWISE. Therefore, UV fluxes would increase with a proper extended source photometry and this would possibly result in a more clear trend, especially at low SFRs at which FUV is expected to be higher, allowing more accurate analyses.

In the comparison of  $SFR_{mircor}$  vs  $SFR_{FUV}$ , in Figure 12, the *mircor* values are intrinsically higher in the lower range. But this is just how this FUV normalization is built; its consistency has to be well assessed in a more expanded sample including a fair number of lower mass galaxies.

In the comparison  $SFR_{FUV}$  vs  $SFR_{RC}$ , in Figure 13, the FUV appears clearly underestimated.

The main consideration is that FUV data was not useful in helping determine which SF calibration to trust at the lower SFRs, where we saw the large discrepancies. This is due to limitations of GALEX photometry as well as the availability of an insufficient amount of FUV information.

## CHAPTER 6: CONCLUSIONS

Thanks to improved WXSC data (T. Jarrett, priv. comm.) and the sensitive Apertif data products, I could do a study of the FIR-Radio SFR correlations for the HI – radio selected sources.

Initially, the aim was to study the reliability of radio SF tracers in dwarf galaxies. When I first estimated the stellar masses using ALLWISE W1 fluxes, the sample resulted to contain a fair number (37/250) of low mass galaxies with  $M < 10^9 M_{\odot}$ . However, using the improved IR photometry (WXSC) only 9 were confirmed in that mass range. Therefore, in absence of a good number of dwarfs, the analysis turned out to be a study of the FIR-Radio correlation for intermediate, high mass galaxies, in the range  $10^9 M_{\odot} < M < 10^{12} M_{\odot}$ .

With the visual inspection, I identified a clean sample of objects for which I believe there is a good agreement between IR and radio traced star forming activity; I put my focus on these galaxies to compare SFRs at different bands.

Whereas  $SFR_{W3}$  and  $SFR_{W4}$  seem to reasonably correlate to the  $SFR_{RC}$ , there is a big discrepancy at smaller values when using  $SFR_{mircor}$  vs  $SFR_{RC}$ . The question now is: which is more reliable? The IR SFR tracers at W3 and W4 may underestimate SF at small regimes because of the lower dust content and opacity; these might also cause a suppressed radio emission. Since the FUV is expected to be consistent at smaller SF values, the point becomes: will the FUV tracer clarify whether to trust more the corrected MIR SFRs over the individual W3, W4 and also RC derived ones?

However, possible limitations of the FUV photometry as well as the unavailability of a consistent amount of FUV data did not allow answering this question. As it remains an open question, further investigations are needed and they would explicitly benefit from a sample enriched in low mass sources.

Overall, to focus the study on low mass galaxies the sample selection should not include the redshift cut-off; moreover, the use of improved Apertif data products could help find a larger number of radio faint objects.

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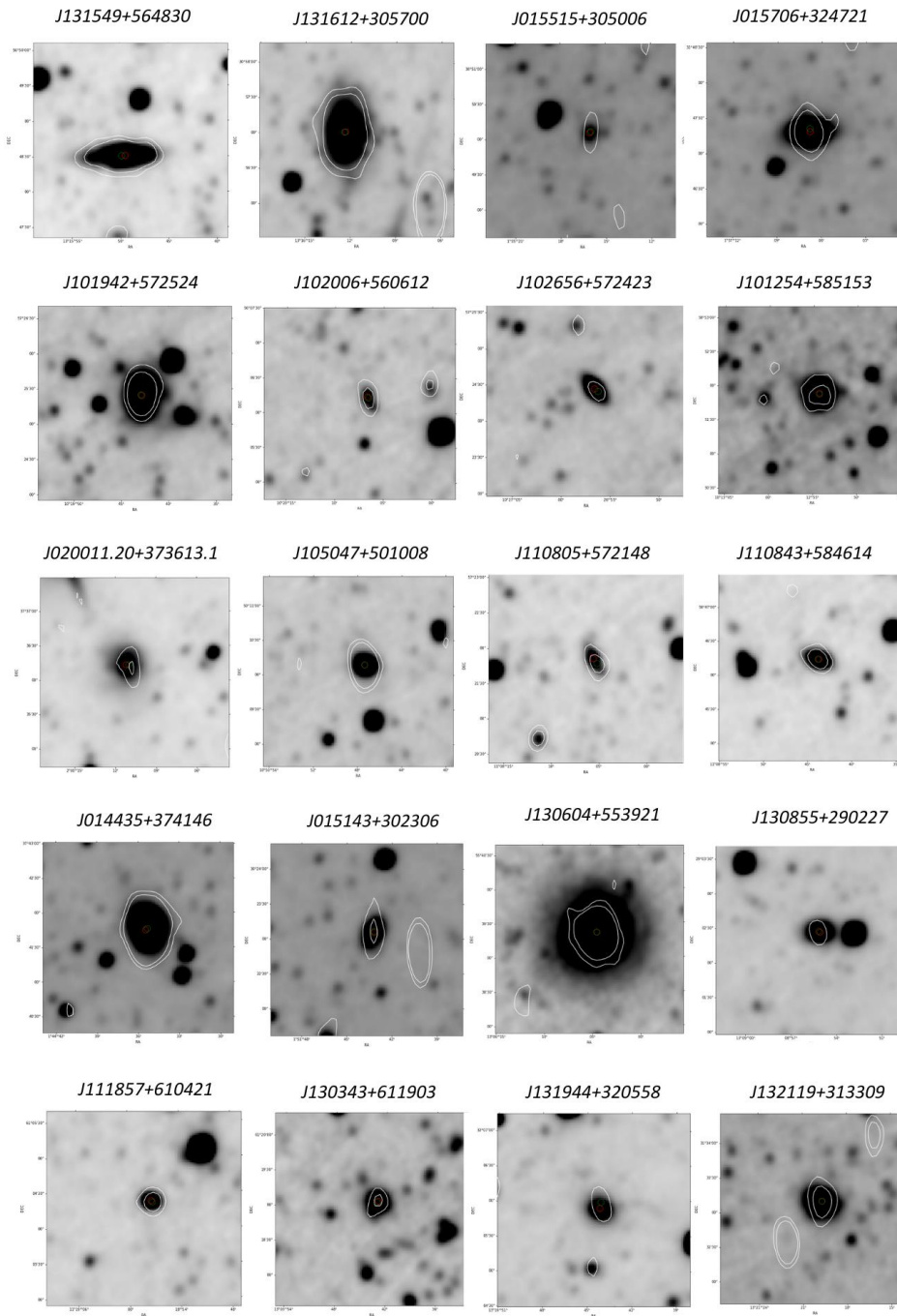
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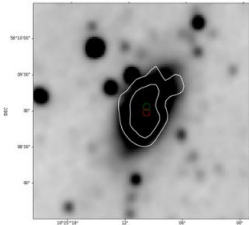
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APPENDIX – VISUAL INSPECTION

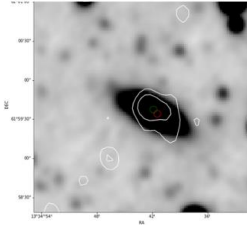
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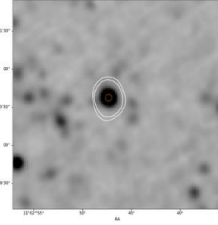
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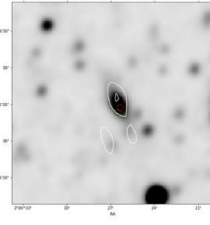
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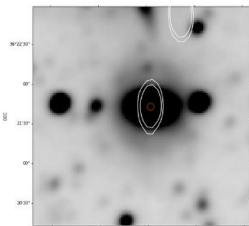
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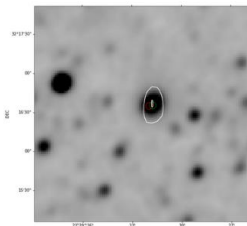
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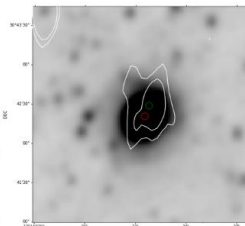
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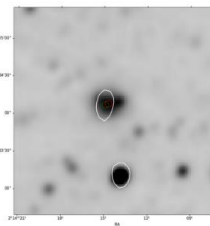
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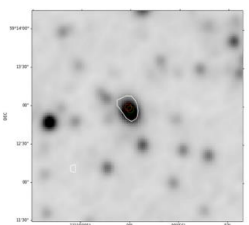
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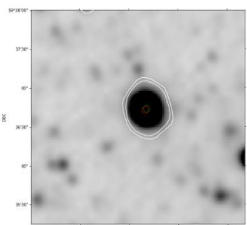
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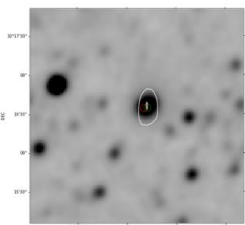
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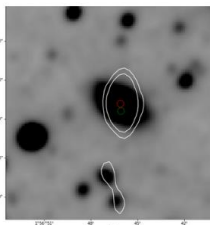
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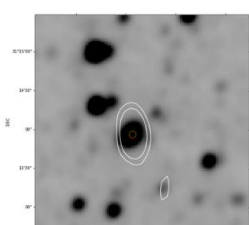
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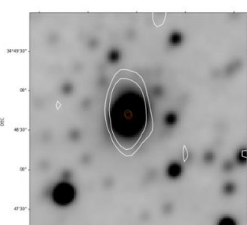
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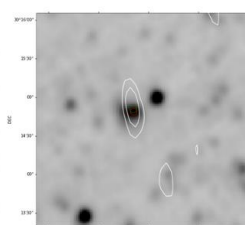
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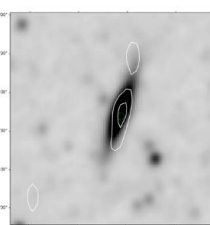
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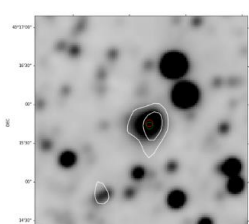
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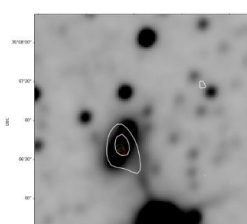
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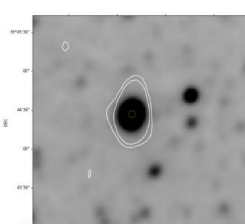
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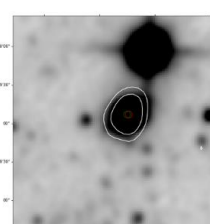
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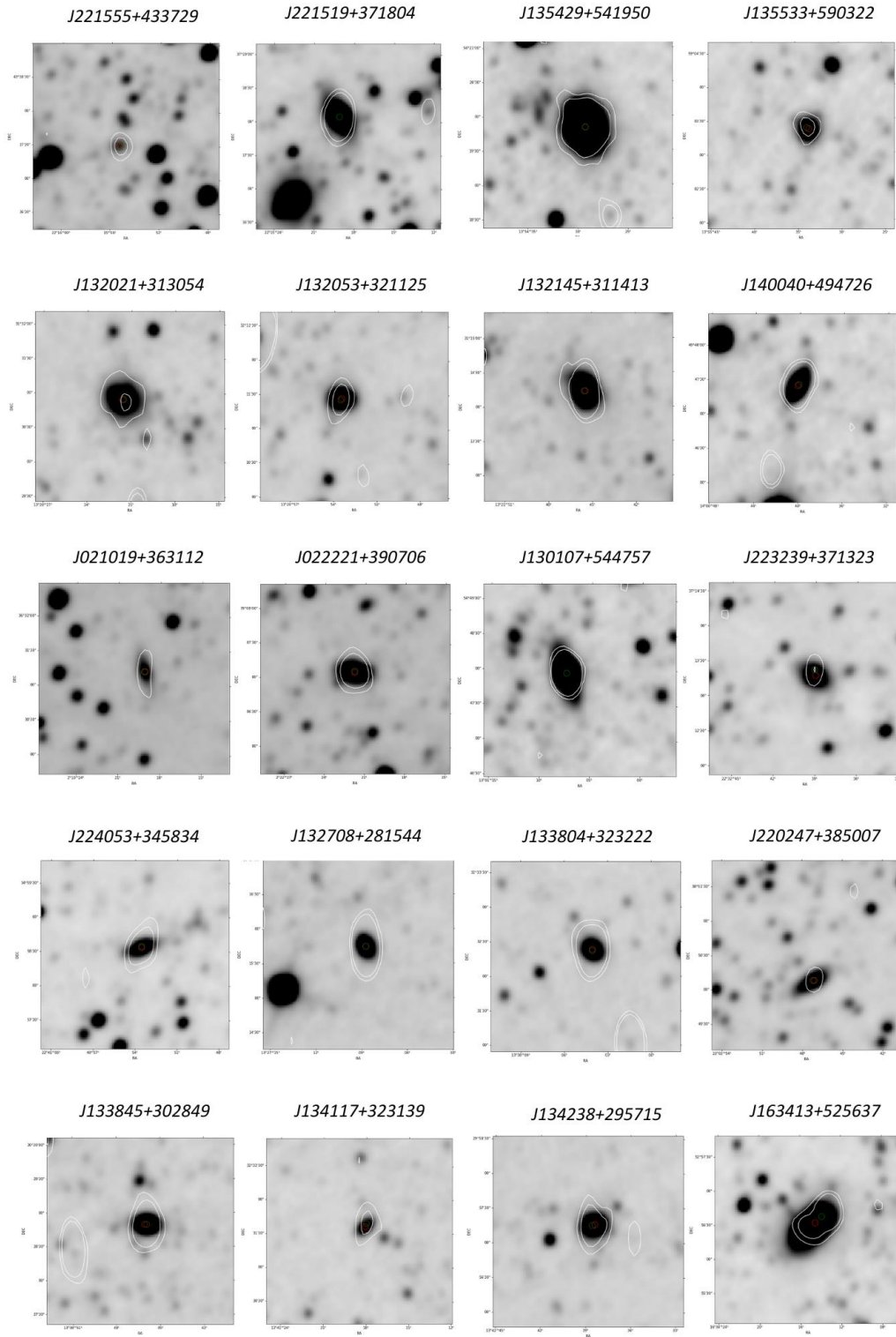


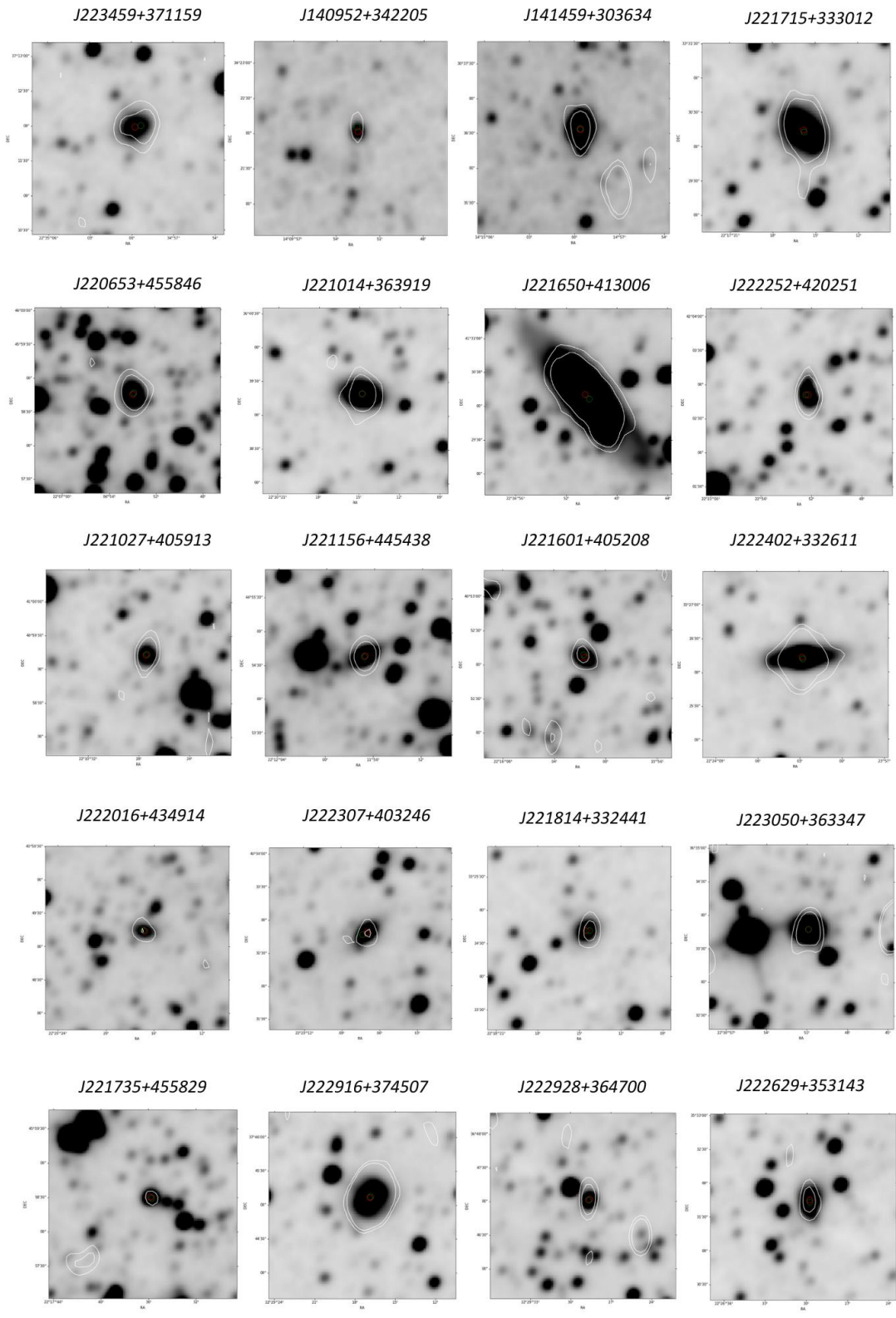
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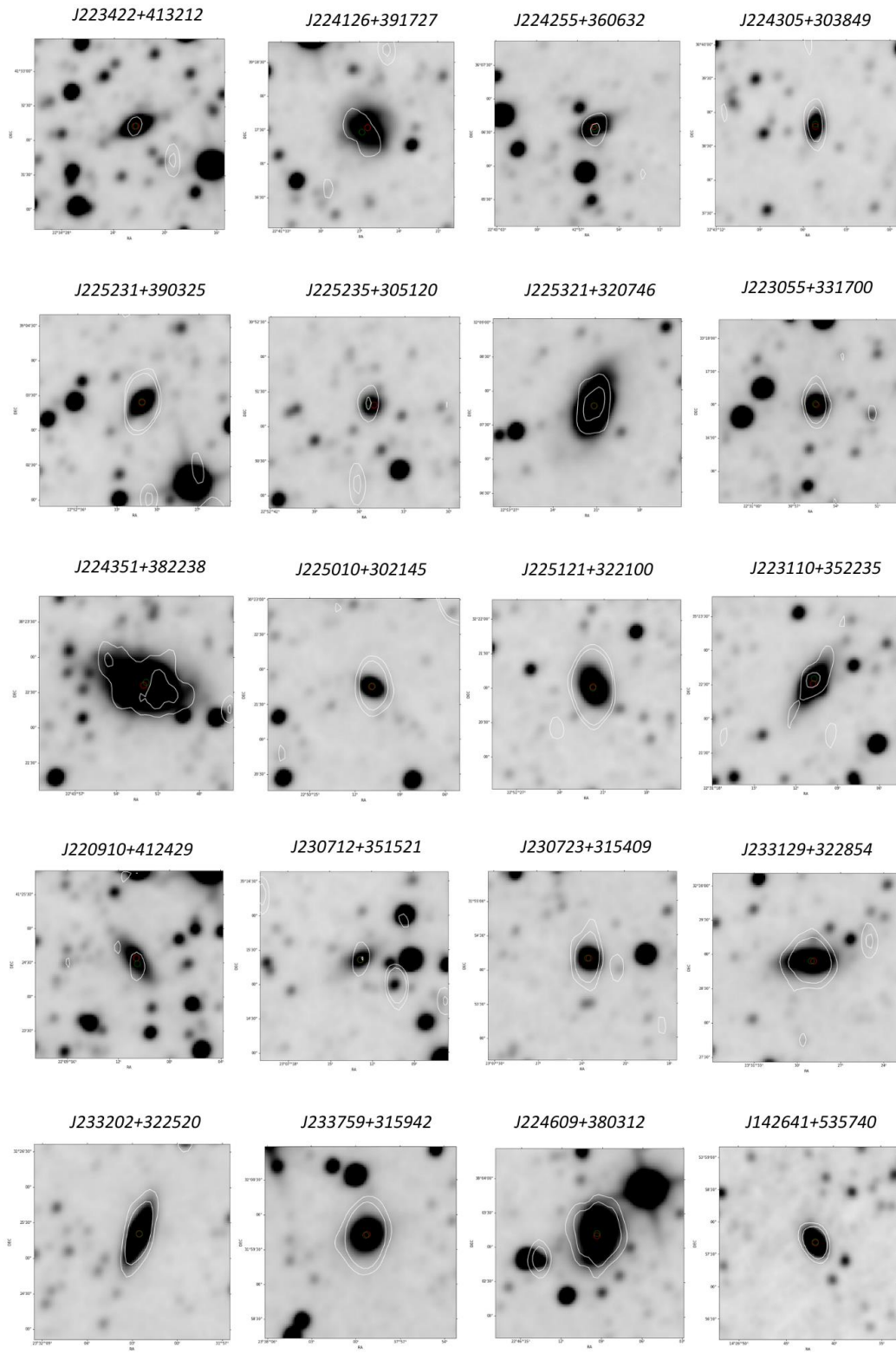
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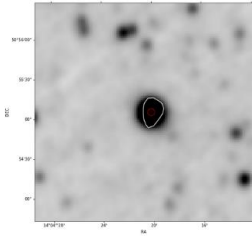




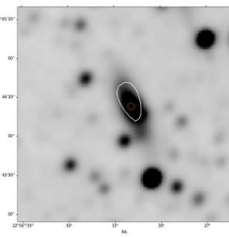




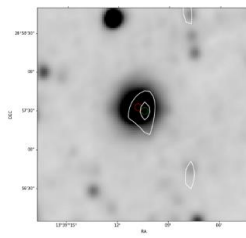
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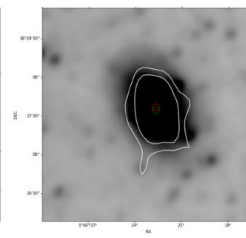
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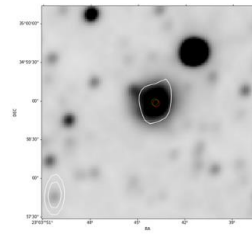
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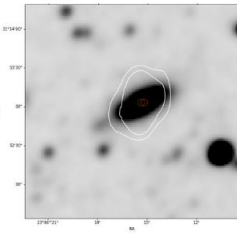
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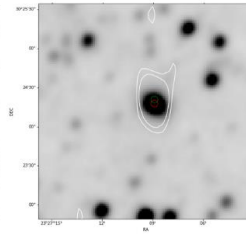
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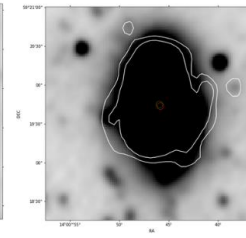
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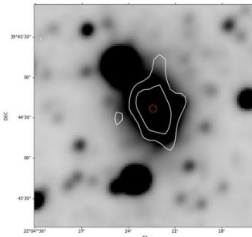
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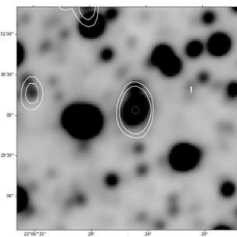
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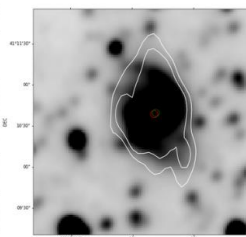
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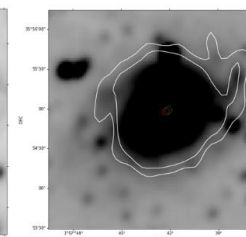
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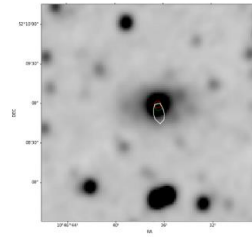
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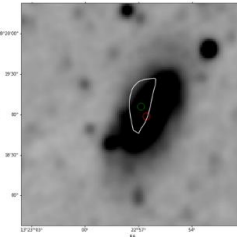
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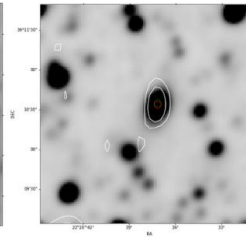
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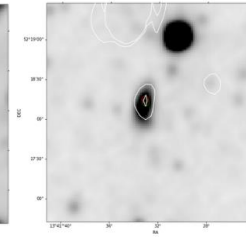
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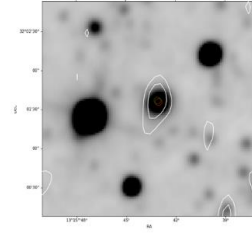
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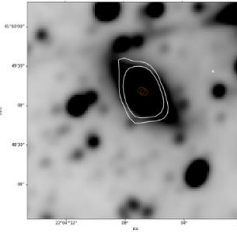
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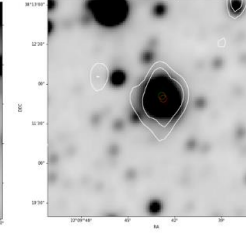
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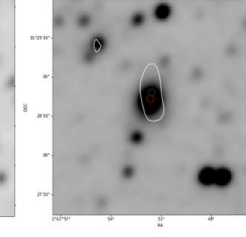
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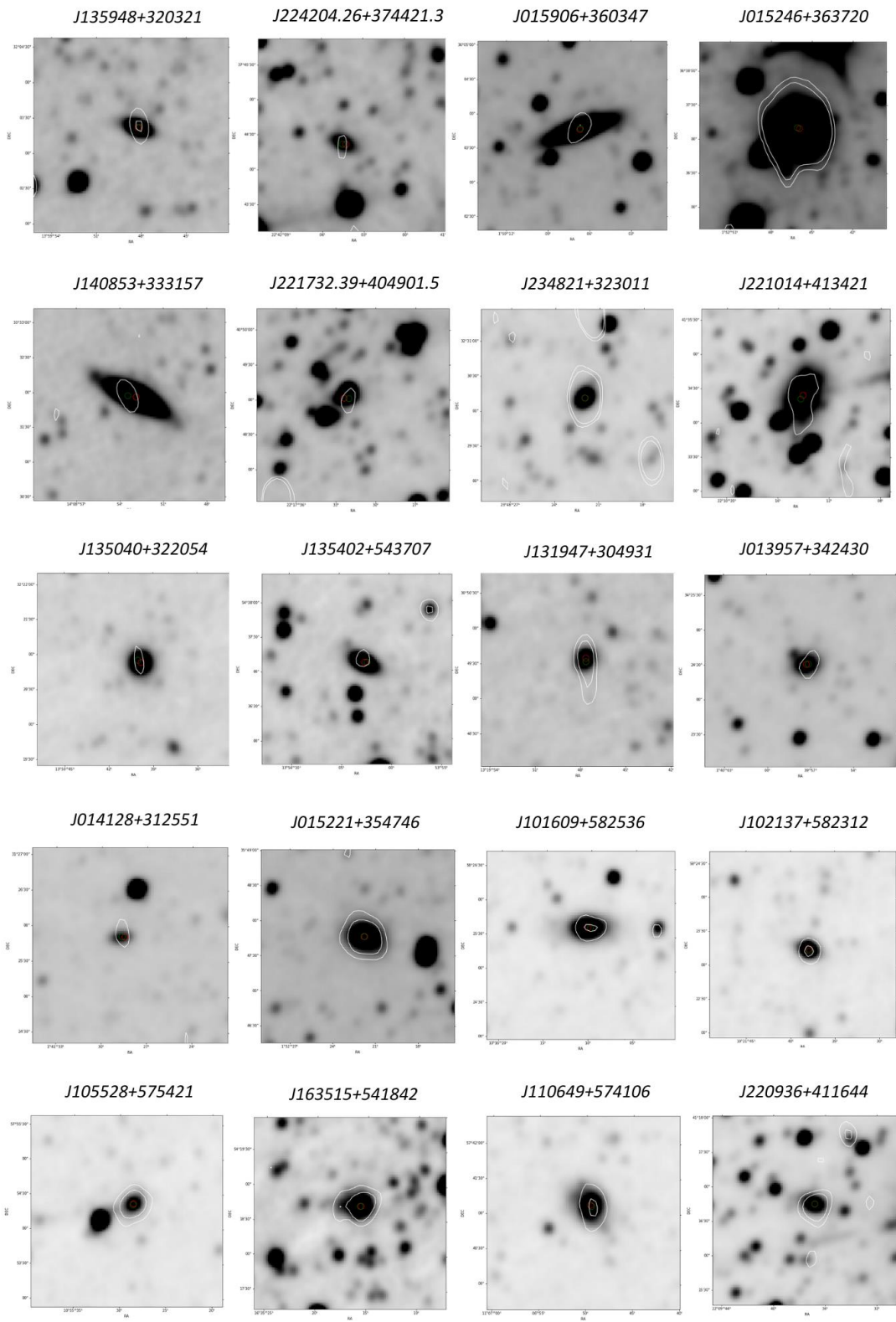


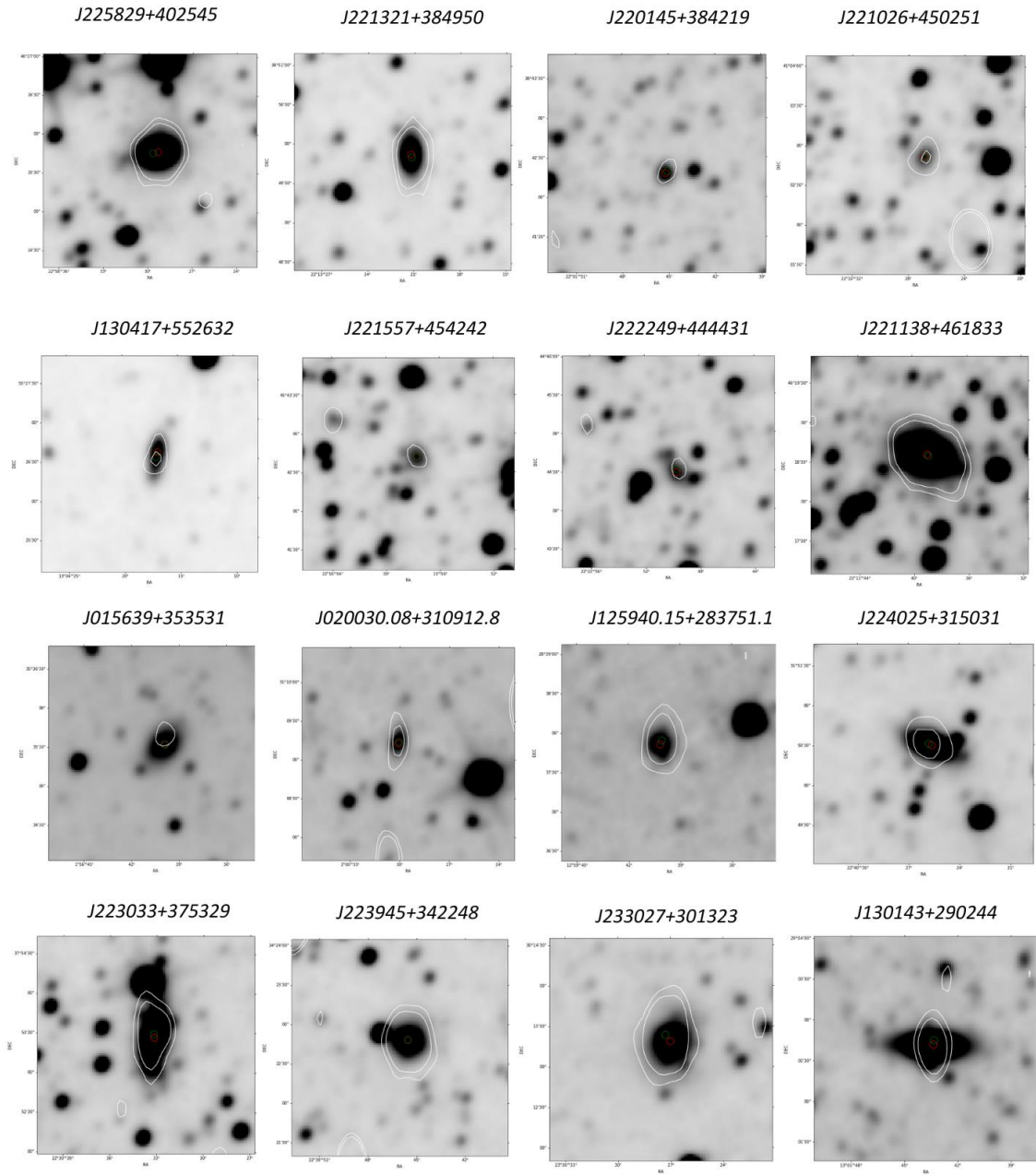
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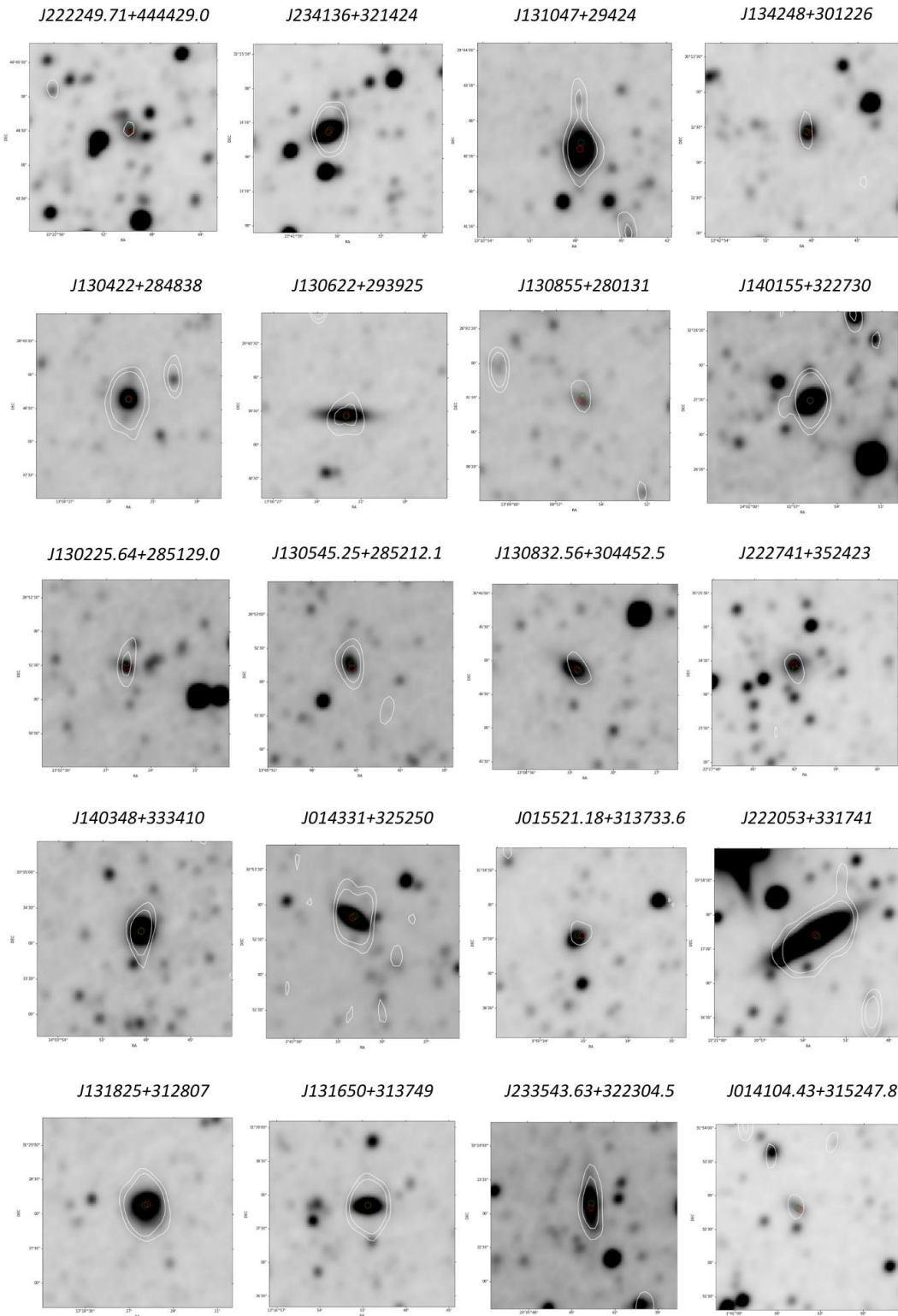
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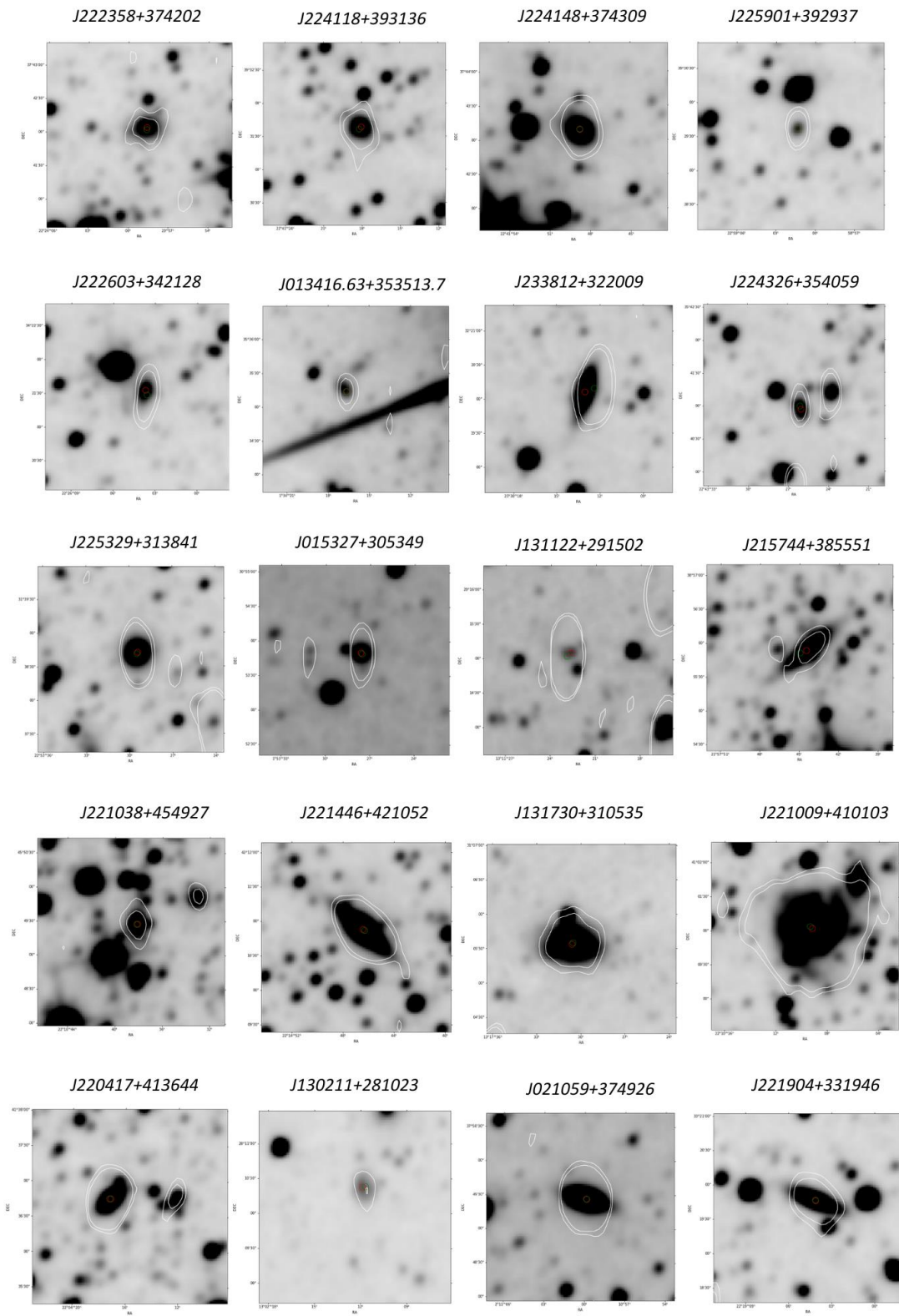




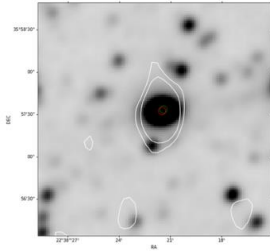


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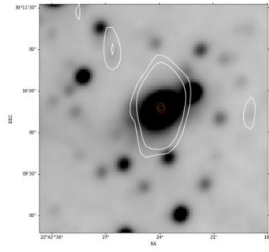




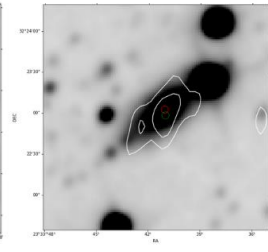
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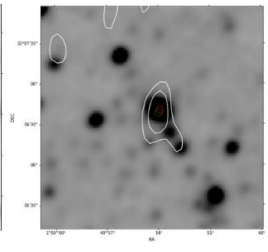
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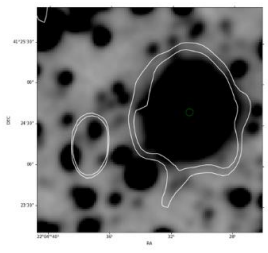
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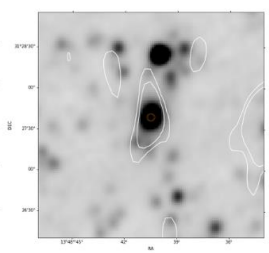
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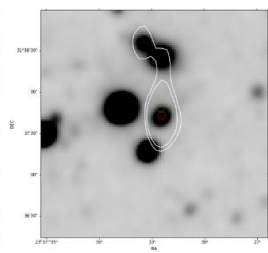
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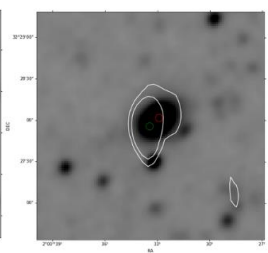
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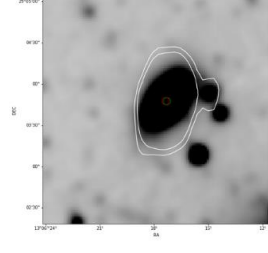
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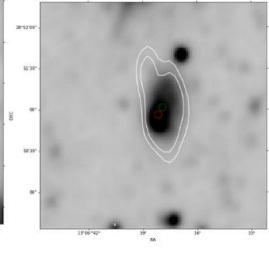
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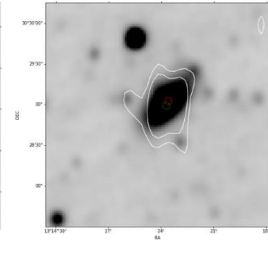
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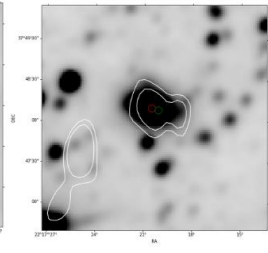
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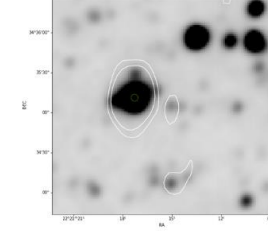
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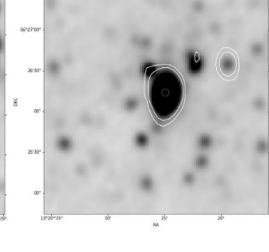
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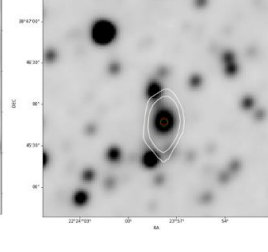
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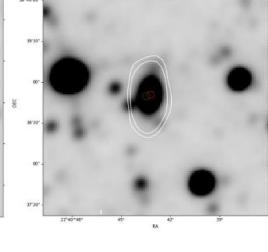
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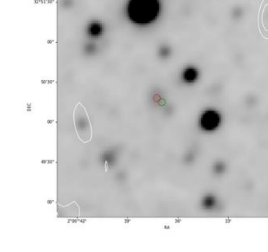
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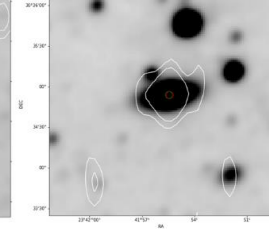
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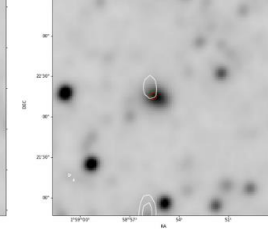
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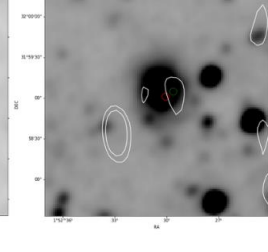
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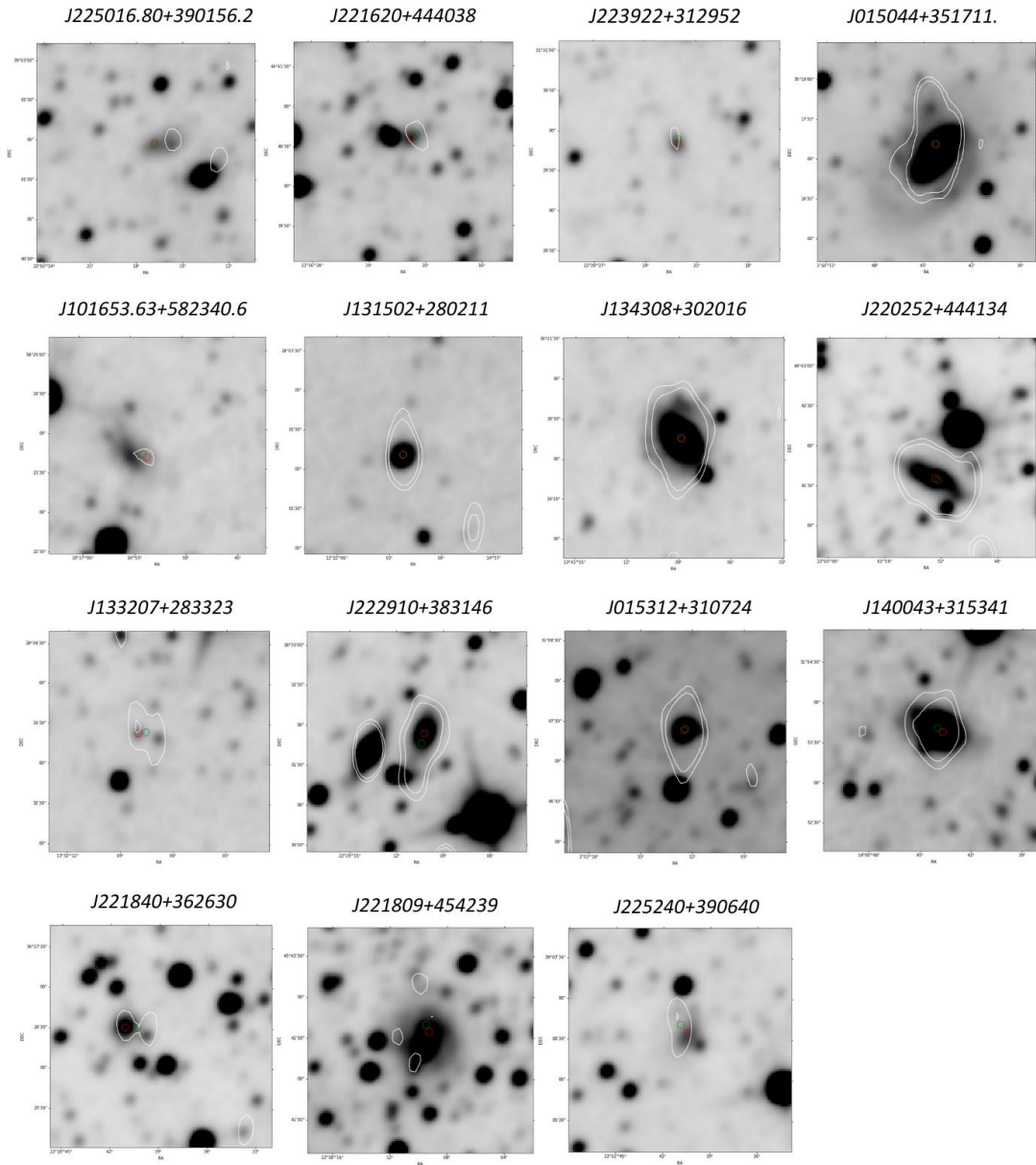


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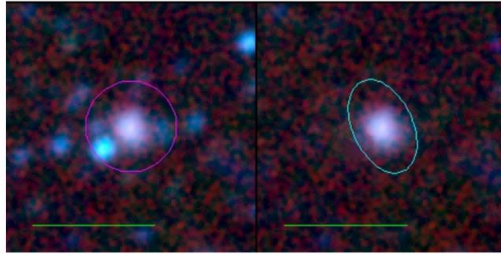
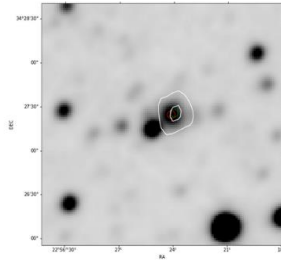




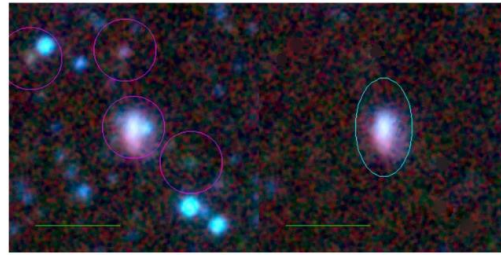
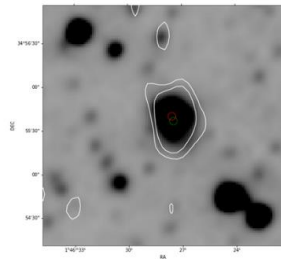


**WISE CONTAMINATION**

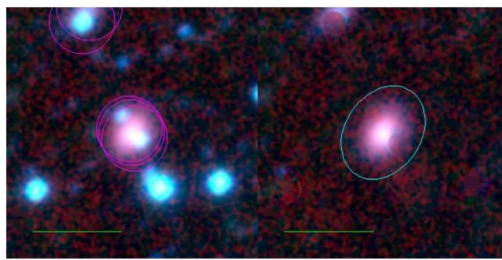
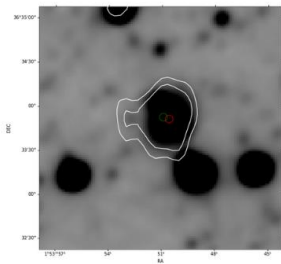
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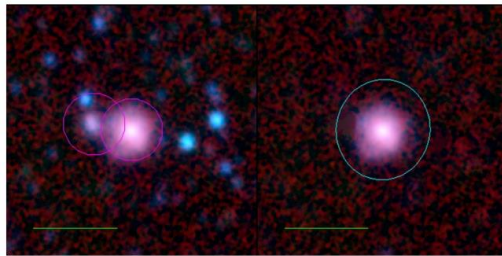
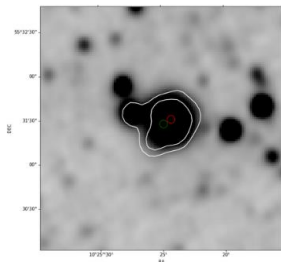
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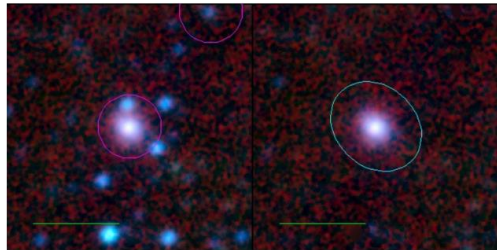
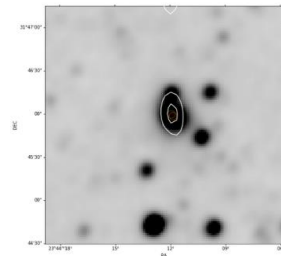
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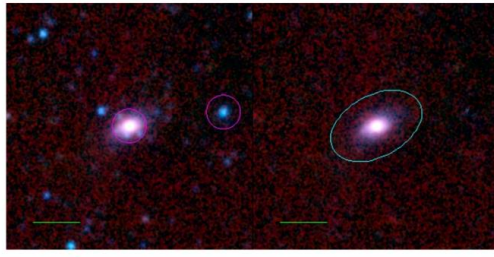
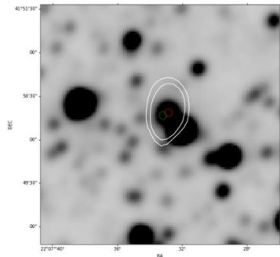
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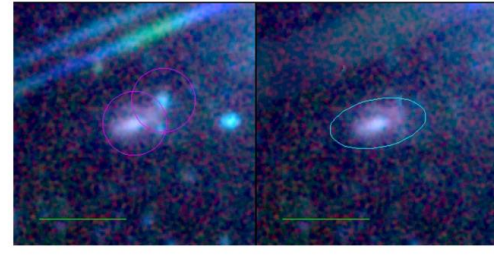
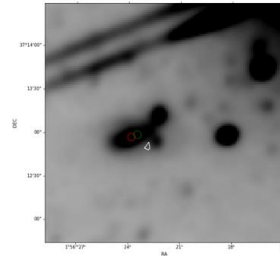
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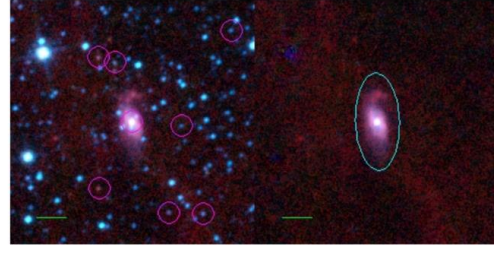
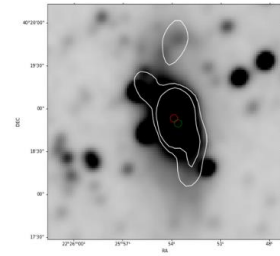
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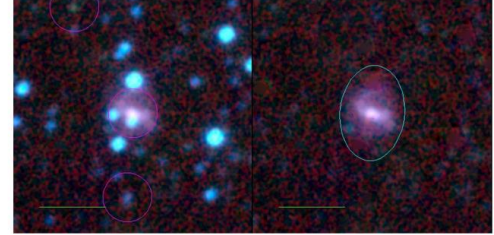
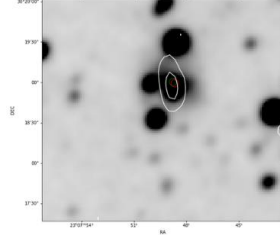
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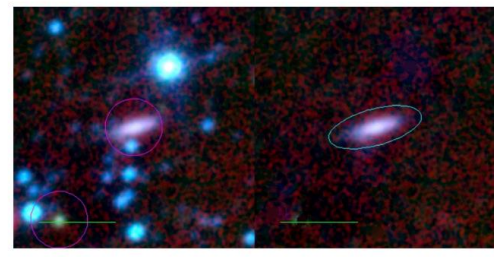
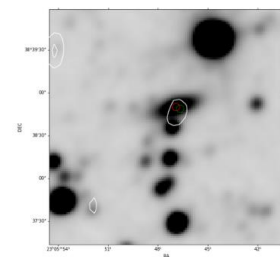
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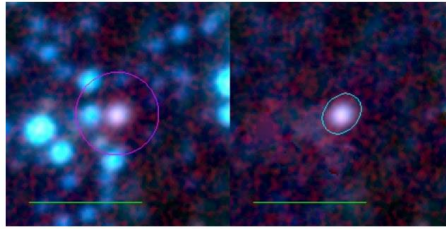
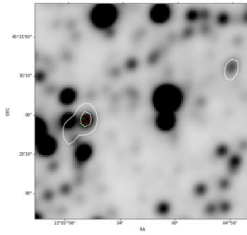
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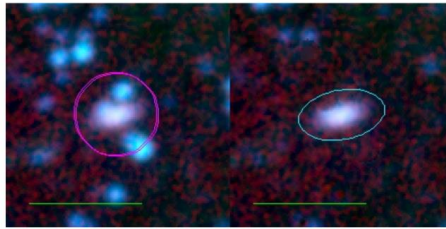
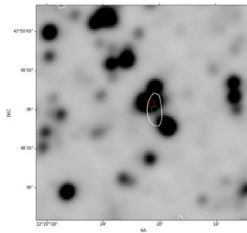
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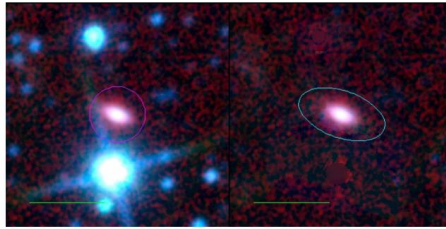
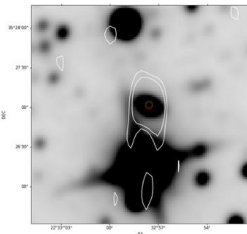
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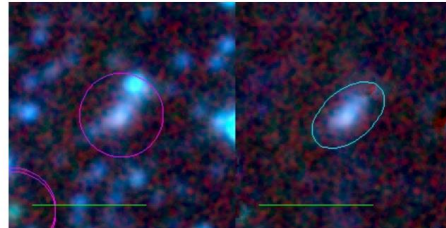
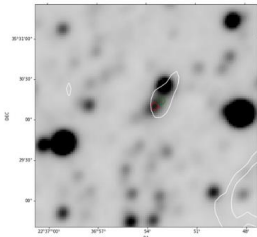
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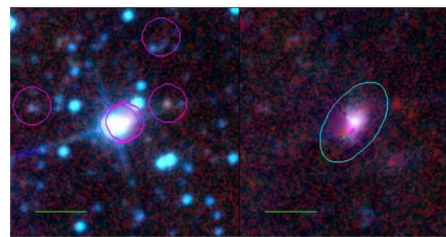
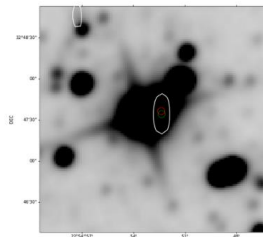
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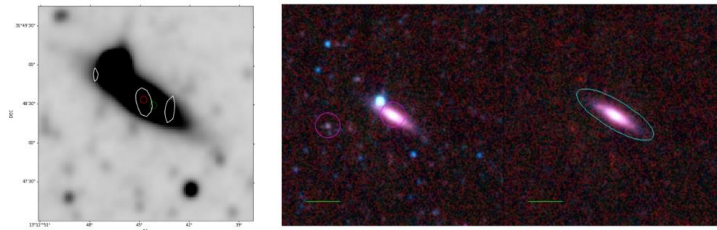
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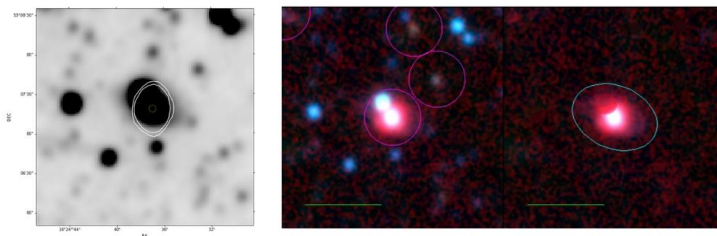
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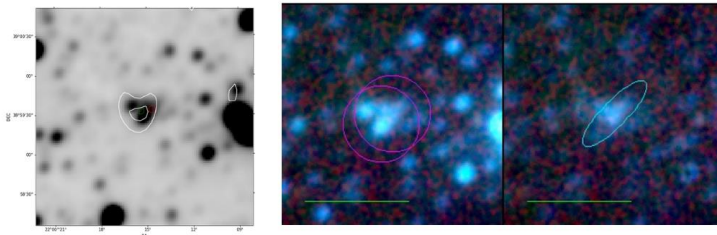
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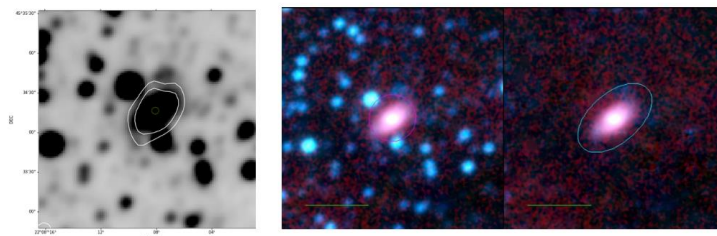
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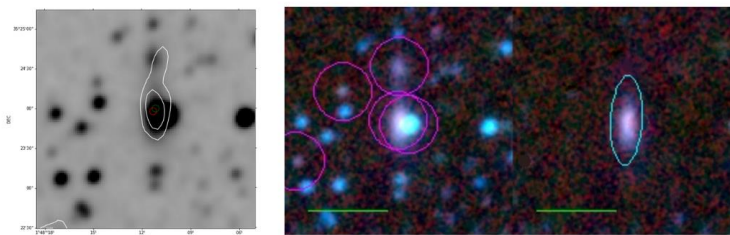
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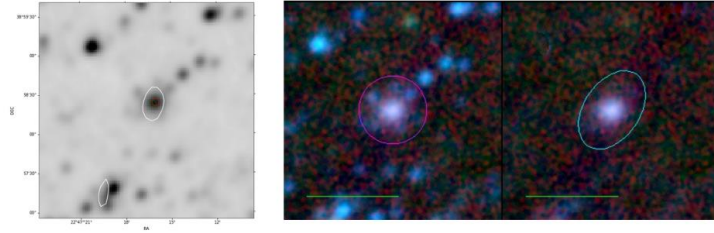
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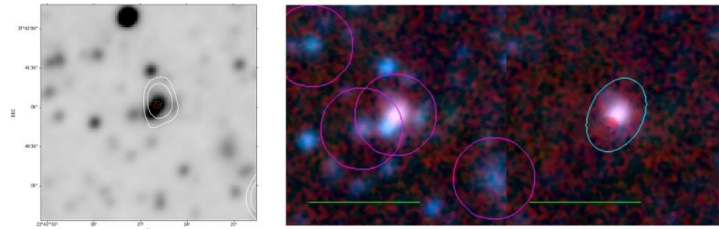
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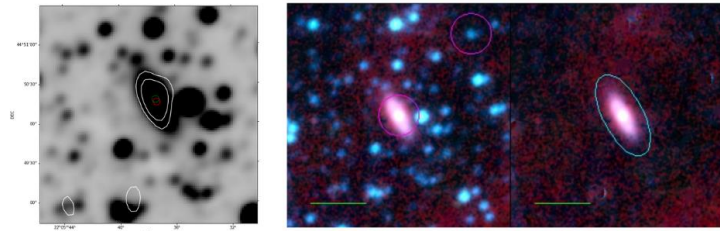
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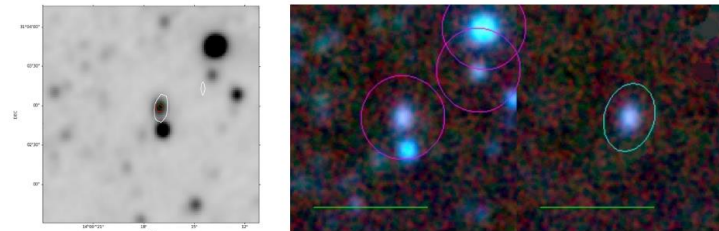
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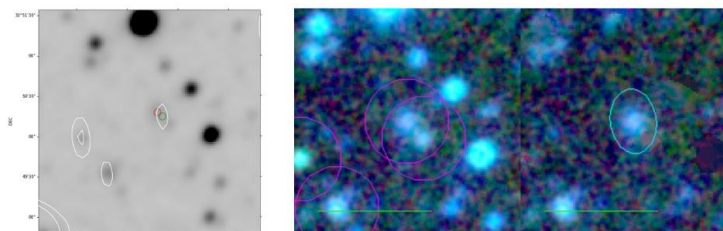
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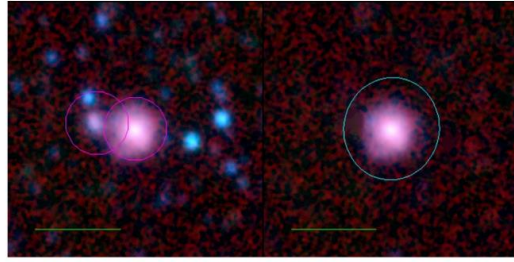
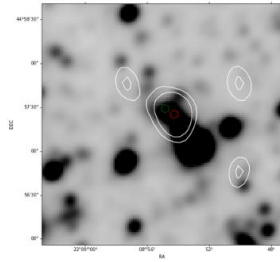
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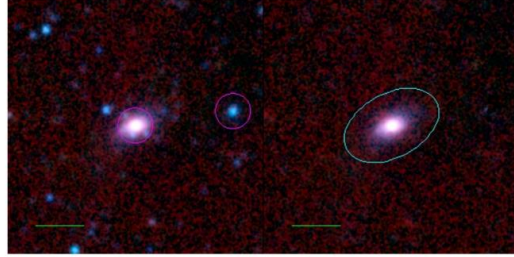
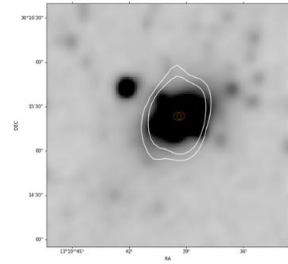
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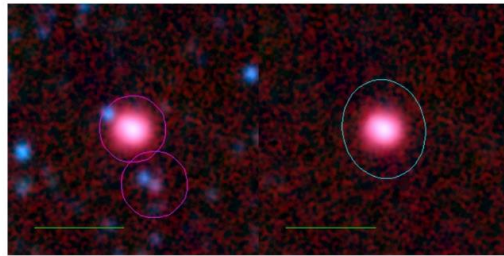
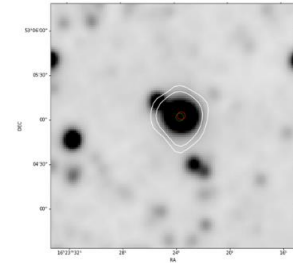
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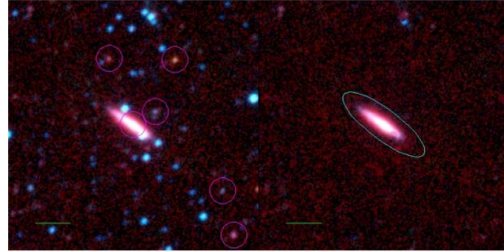
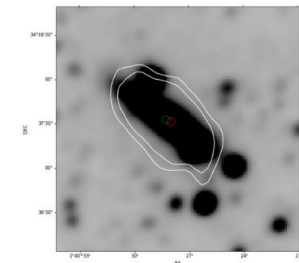
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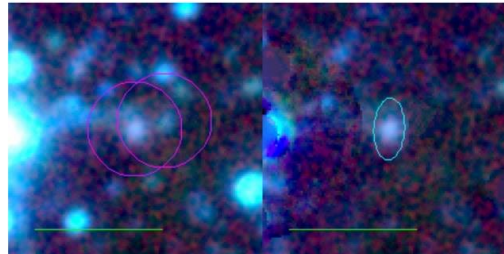
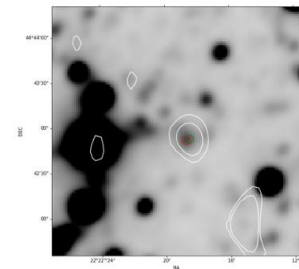
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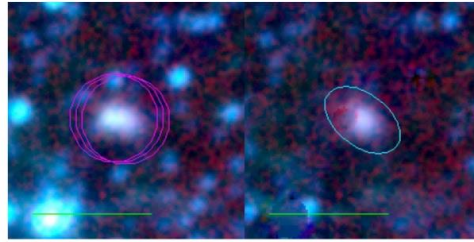
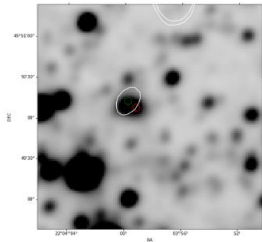
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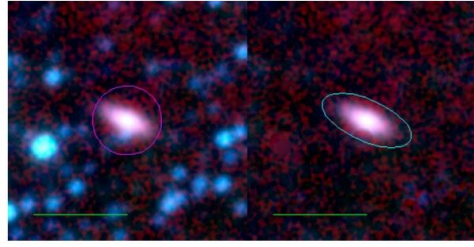
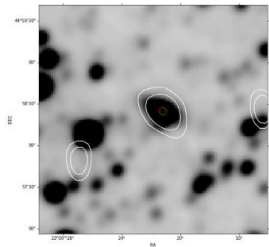
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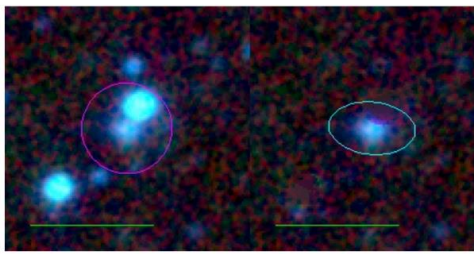
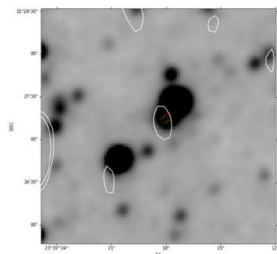
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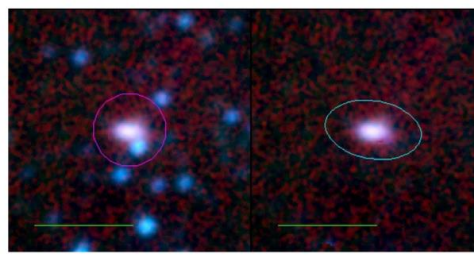
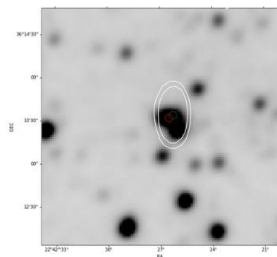
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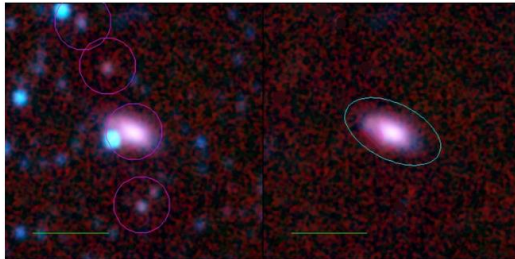
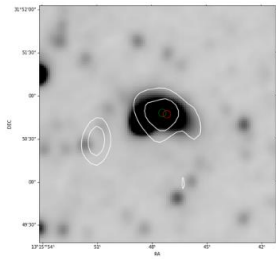
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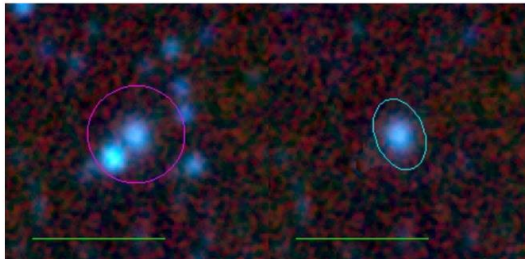
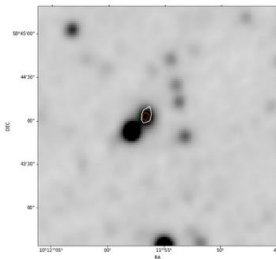
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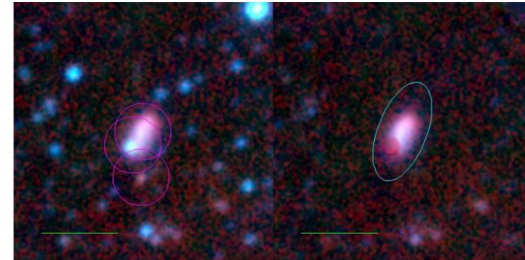
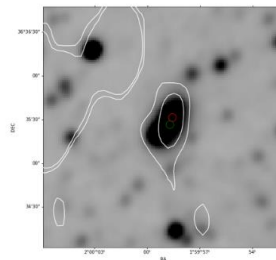
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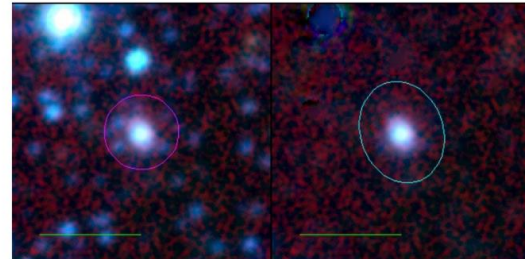
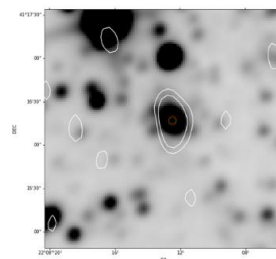
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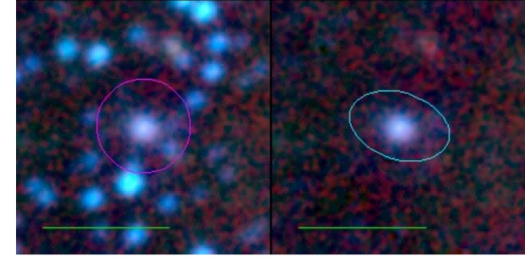
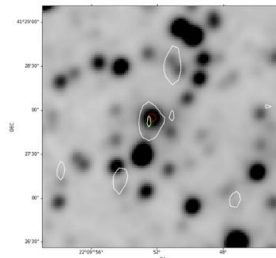
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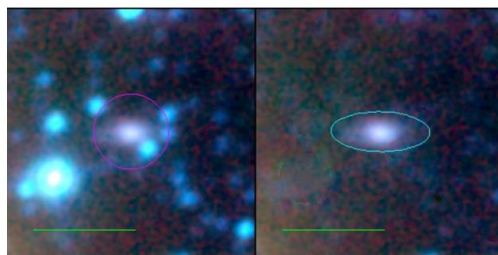
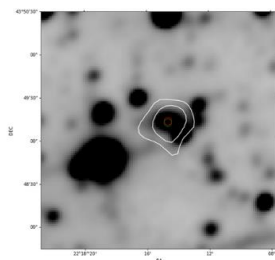


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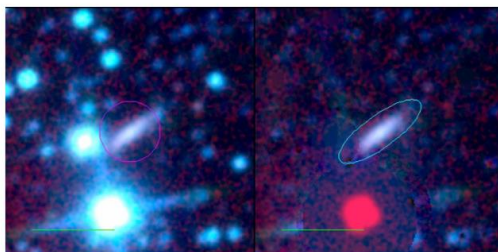
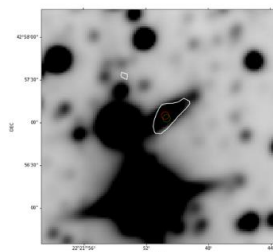




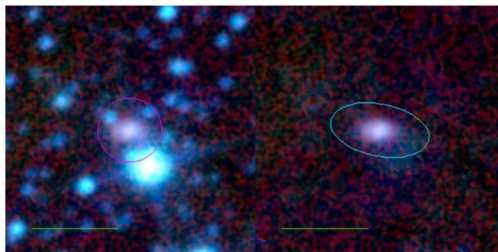
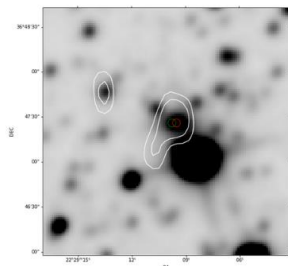
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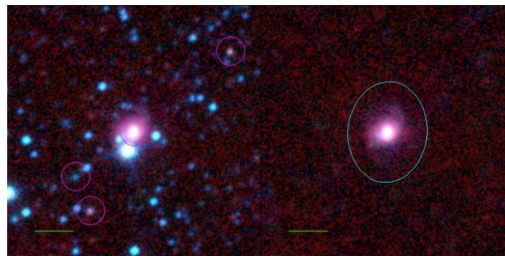
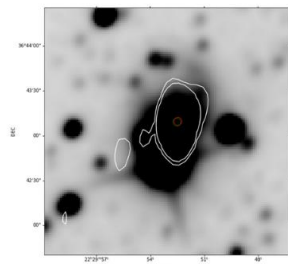
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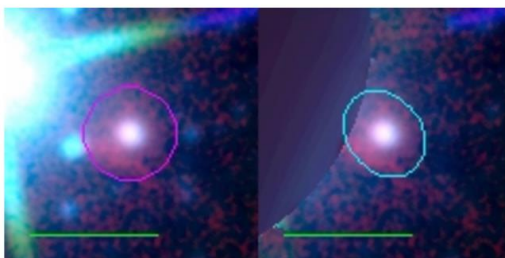
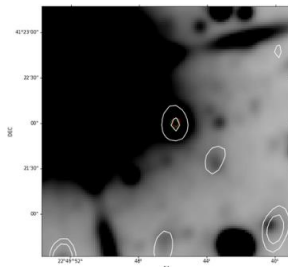
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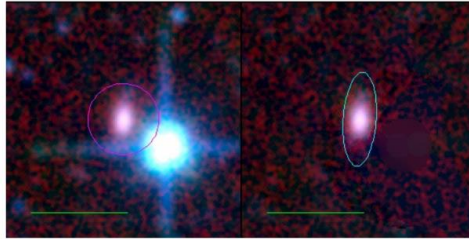
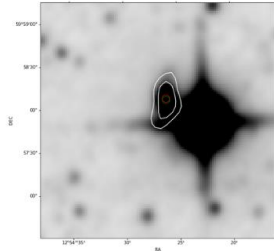
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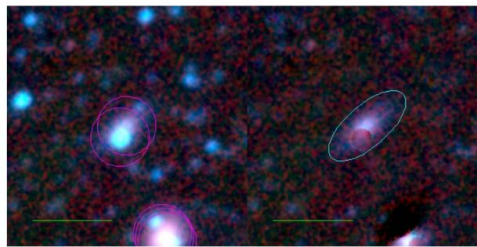
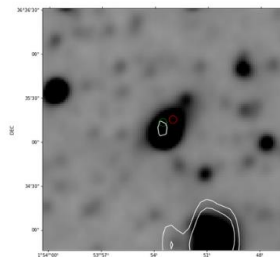
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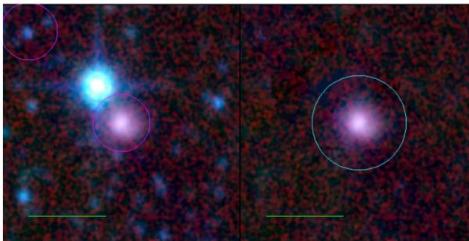
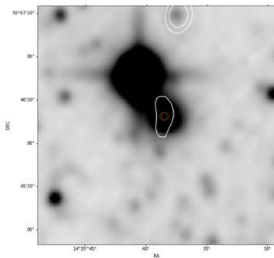
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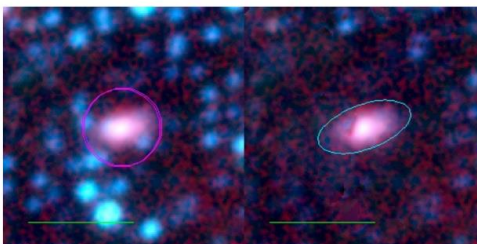
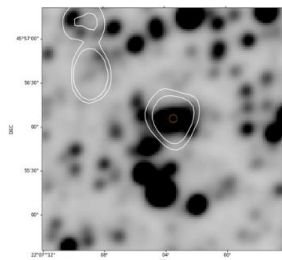
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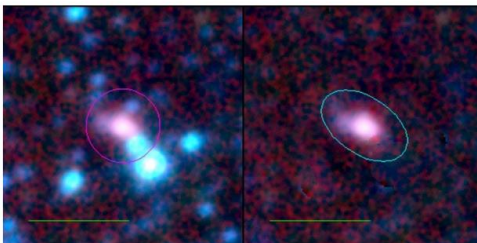
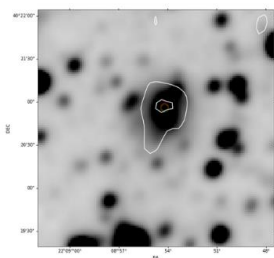
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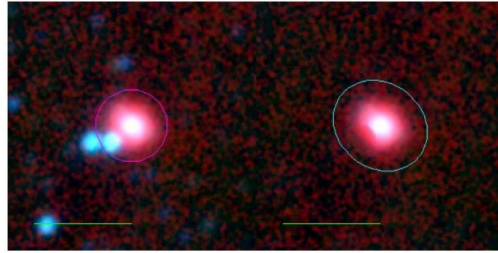
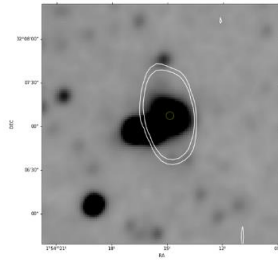
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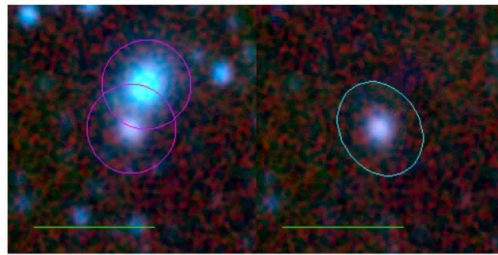
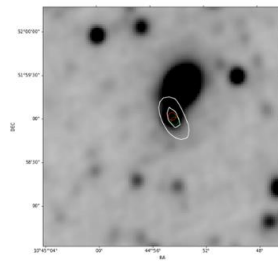
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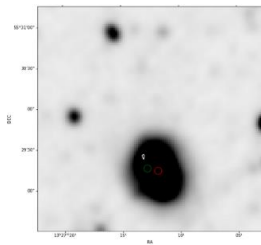


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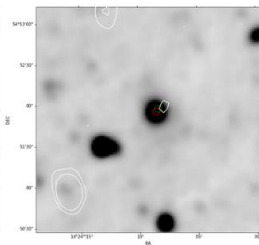


**BAD MATCH**

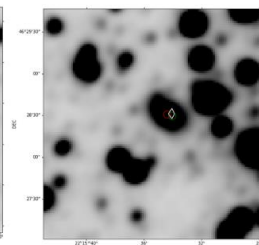
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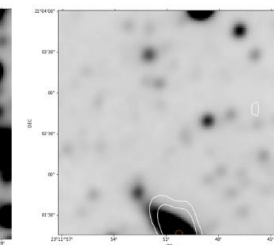
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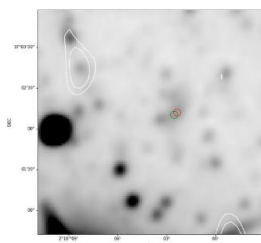
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*J231150+310116*



*J021002.41+370212.7*



*J224731+403402*

